

sufficiently of late experimented, by our Partners, that haue
vled Leuant.

Peraduenture there are some will saie, that he knoweth a
good Compasse, if he see it. I saie the Compasse maie bee
good, and yet not good for hym, except his Plat bee agreeable.
As for example. A Leuant Compasse is a good Compasse, to
vse with a Leuant Plat, but it differeth from our Compasse
halfe a point more Easterly. And others there are of Dansk,
that differ from ours $\frac{1}{2}$ a point more Westerly, and yet bee-
ing vled in their kinde, are good Compasses.

And therefore I conclude, that generally the beste Com-
passe is this sort set at $\frac{1}{2}$ a pointe, because the maior parte of
Compasses and Plattes, doeth not differ from this about $\frac{1}{4}$ of
a point, except the rime alone named of Leuant and Dansk.

I haue be-
Southward
force, and to
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by beeyng long auient from the Stone, for not veyng touched
or refreshed therewith. And again, the Pinne that beareth the
Flie maie bee so dulled with long vsing, that the Flie is as it
were staid, that it can not plaie as it would if it were sharpe.

Therefore, if you make it sharpe with a Whetstone, you
shall finde it remedied: and also when you finde it light, or too
tickle, you maie dull the point of the Pinne, with the leafe of
a paire of writyng Tables, untill you maie see the top
thereof, and then the Compasse will bee better for

a high Sea. And thus by sharpyng and dul-

lyng of the Pinne, you maie make

your Compasse fit for all

Weathers.



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A DISCOVERS
of the Variation
of the Cumpas, or
Magneticall
Needle.

Wherin is Mathematically shewed,
the maner of the obseruation,
effectes, and application
thereof, made by
W. B.rough

And is to be annexed to
The newe Attractiue
of R. N.

1581.





To the Trauelers, Seamen, and
Mariners of Englande.



Auyng of late (gentle reader) recei-
ued from the expert Artificer Ro.
Norman, his booke intituled The
newe Attractive (who of the great
good will, and affection he beareth,
hath attributed in his dedication, that, whiche I
acknowledge not to bee deue) in the whiche amon-
gest other diuers vertues and properties of the Ma-
gnes or Lodestone, he intreateth of the declining of
the Needle touched therewith from the plaine of the
Horizon, (a matter neuer before found, or written of
by any). For the further behoofe and benefite of all
traueilers and Seamen, I tooke occasion to inlarge the
same with this discourse of the variation of the Com-
passe, wherein I haue handled the whole varietie of
that subiect, bothe Practically, and Mathematically,
to the ende I might partly satisfie bothe the vulgar,
and also the learned sort. For, knowing the variatio
of the Cumpasse to bee the cause of many errours and
imperfections in Nauigation, and perceiuyng that all
those that haue as yet gone about to giue rules in that

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arte,

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arte, haue left this (beyng a principall point, and euē the grounde of all the reste) vntouched, or at least so sleightly handled the same, that little or no benefit could be gathred therby: I haue here set doune the sundrie waies to obserue the same at all tymes & places, that the inconuenience beyng knowne, might be considered of, and auoided. VVherein, although my cheefest intent hath been to p'ease those that shall haue occasion to put the thyng in practice by their owne trauaile and experience, yet because some of the rules are deducted from the fountaines of the Mathematicall Sciences, and wrought by the doctrine of Sines and Triangles, whiche maie seeme strange in our Englishe tongue, & wherewith fewe Seamen are yet acquainted, I maie seem to haue missed of my first good meanyng, but I would wishe them to chuse that whiche is plain, and conformable to their capacities, and make their profite thereof, and for the reste vnderstande, that of suche obseruations as thei them selues can not presently applie to the purpose, by others that are thoroughly instructed in these Mathematicall supputations, or by them selues when thei shall attaine to the knowledge therof, maie be inferred suche effectuall matter as is by these rules and preceptes promised. VVherefore I would haue all Seamen to vse suche diligence in
their

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their trauailes, that no oportunitie be omitted, when,
or where any obseruation maie be made, either for the
variation, or latitude of places, or of any other neces-
sarie pointē incident to Nauigation, and thereof to
keepe continuall notes & memoriall. For these obser-
uations, there needeth not many troublesome Instru-
mentes, onely for the variation, the newe Instru-
ment in the ende of this treatise I preferre before all
other. And for eleuations, a plaine Astrolabe exactly
made, and a crosse staffe, are sufficient. (The Globe
were also a verie good and necessarie Instrument. for
besides many pleasaunt conclusions that maie be tried
by it, it doeth lighten verie muche the conceiptes, for
vnderstandyng diuers important pointes, but it is
too troublesome [or otherwise not fit for euery Ma-
riner] to be caried to the Sea). Vnto the whiche maie
bee added the Topographicall Instrument, for taking
of distances, and making descriptions vpon the land.
With these Instrumentes, and the sailyng Cumpasse
and Marine plat, (whiche are alwaies to be vnder-
stoode the principall, and moste necessarie Instrumen-
tes for Nauigation, for by them onely any voiage
maie bee made, but without them no Nauigation can
bee performed.) the whole worlde maie bee traueled,
discovered, & described. These are sufficient for a per-

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fette Mariner, and more then these were superfluous, onely the runnyng glasse, leades, lines, and such like appendances of the other excepted.

But to haue all these Instruments, and not to vnderstande the groundes how to vse them, were a great Vanitie. Therefore I wishe all Seamen & Trauellers, that desire to bee cunning in their profession, first to seeke knowledge in Arithmetike & Geometrie, whiche are the groundes of all Science and certaine artes, of the whiche there is written in our English tongue, sufficient for an industrious and willying minde to attain to greate perfection, whereby he maie not onely iudge of Instrumentes, Rules, and preceptes given by other, but also bee able to correcte them, and to deuise newe of hym self And this not onely in Nauigation, but in all Mechanicall Sciences. As by the studious practise and exercise in these artes, haue attained to rare and singuler knowledge: In Architecture, Vitruuius the Romaine: In paintyng that famous Germaine Albertus Durerus: And in buildyng of Shippes, Matthew Baker our countryman: And others in other faculties as thei haue been mooste skilfull herein, so haue thei excelled. Hauyng these helpes and groundes with the Instrumentes before specified, a Mariner maie bee able to make description in platt of the coastes

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Isles and Countreies, and of the Banckes, Rockes, and
Shoaldes in the Sea, with the deapthes and other ne-
cessarie notes obserued in his owne trauailes particu-
larly, & effectually accordyng to the truthe, (whiche
is the cheefest parte required in a perfect Mariner.)
And not be alwaies tied to the reportes of other, or to
the Portugale, or Spanishe Marine platts, whiche are
made by the Cardmakers of those Countreies, men that
are no travelers them selues, but doe all thinges ther-
in by information, and vppon the credite of others,
whiche onely committ to memorie the forme and ma-
ner of the Sea coastes, with making some fewe notes of
the lying of one place from an other, whiche can neuer
bee so perfecte as the descriptions that are made vpp-
on the present sight and viewe of places, albe it he be
neuer so skilfull and cunnyng, that shall so cary the
same by memorie, how muche lesse then by the un-
skilfull. By this meanes the Cardmakers set doune
thei knowe not what: as maie appeare by the descrip-
tions of their owne coastes, whiche are verie grossely
and vnperfectly dooen, whereas the Marine plattes
ought to bee described by suche as can giue reason, and
shewe obseruation of euery particularitie contained
in the same, as well for the latitude of places, as the li-
ying by the Compassse of the Capes, Headlandes, Poin-
tes

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Etes, Flandes, Baies, Rockes, Sholdes &c. one from another, and the distances betweene them. The errors of those descriptions, I maie not attribute to the Card-makers, but to the vnskilfull Seamen of those countries, for if thei were otherwise, as thei haue been accounted the moste skilfull of the worlde, those errors could not haue continued as thei doe: true it is that for their great trauailes, thei haue been worthely famous aboue all other nations, till now at length our Countryman Sir Francis Drake for valorous attempt, prudent proceeding, & fortunate performing his voiage about the worlde, is not onely become equall to any of them, but in fame farre surmounteth them all. But those Cardmakers, and all other that collecte and gather Hydrographical, and Geographicall descriptions of other mennes trauailes or reportes: as their paines maie bee greate, and deserue due commendation, so their doynge maie bryng commoditie diuersely. And in this behalf Abrahamus Ortelius in his Theatrum, hath deserued immortall praise, for collectyng together, and reducing into one comodious volume, the diuers plattes and descriptiōs, made by diuers and sundrie men. But amongst all those that haue made Geographicall descriptions, I can not a little maruaile at Guilielmus Postellus, who beeyng a famous learned

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ped man, a greate traueiler and Cosmographer, and Deane of the Kynge's Professors in the Vniuersitie of Paris, in his Vniuersall Mappe. Anno 1520. besides that it is generally bandeled after suche a grosse and confused maner, that it might seeme rather to haue come from some rude vnskilfull, then from hym so famous a Doctor; hath also in the imagined Countries aboute the North Pole, so corrupted it with his fowle dreames, and fantastickall inscriptions, attributing to those supposed landes, diuers people, as the Georgians and Hyperboreians, and assignyng there to be the highest hilles of the worlde, and the people dwelling on the, to haue the continuall light of the Sunne; Sueta Zemlia founde by the Englishemen, An. 1550. the holie Lande, the place of the cheefest felicitie, the Hyperborean feeldes, and therefore the felicitie of the Moluccas, with many other ridiculous absurdities: That by the grosse errors of this learned man in these matters, I am taught, that what so euer fame goeth, or opinion is conceiued of any man for profound learning, and smother deliueying of their conceiptes, on what so euer greate promises are by them selues made in these artes, to iudge of them accordyng to the woorkes that come from them, and not other wise to bee deceiued.

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For auoidyng prolixitie in this my Preface to so
smala volume, I referre the gētle reader, to the worke
it self. Yet by the waie it shall not bee a misse, that I
commende vnto you, the table of the Sunnes declina-
tion (or Regiment) made by R.N. which is calculated
for the present tyme, and differeth not from the truth
in any place aboue one minute, wheras in all other be-
therto made and extant, there are great errors. Ther-
fore, suche as other wise can not from tyme to tyme
calculate their declinations, accordyng to the place of
the Sunne to bee giuen by the Ephemerides, and table
of declination of Reinholdus maie boldly vse this
Regiment for 20. yeres without any sensible error.
And so wishyng my trauailes in this treāse maie doe
suche good as I ment, I commit the same to
your gentle constructions, and your sel-
ues to the Almightye. At Lime-
house the 26. of Septem-
ber. Anno 1581.

William Borough.





A Table of the Chapters con- tained in the treatise.

¶ The first Chapter.

OF the Variation of the Cumpas, or magneticall Needle.

¶ The second Chapter.

The manner how to vse the Instrument of Variation.

¶ The third Chapter.

How to finde the Variation of the Cumpas or Needle at any place, the eleuation of the Pole, and situation of the meridian vnknowne.

¶ The fourth Chapter.

The eleuation of the Pole, and place of the Sunne giuen, how vpon the Globe, to finde the Variation of the Needle, by any one obseruation, either in fornoone or afternoone.

¶ The fifth Chapter.

How to finde the Variation by Arithmeticall calculation, vppon any one obseruation in fornoone or afternoone, the latitude of the place, and declination of the Sunne being giuen.

¶ The sixth Chapter.

An other way most generall, how to finde the Variation by one obseruation, either in fornoone or afternoone, the eleuation of the Pole, and declination of the Sunne being giuen.

The seventh Chapter.

To finde the eleuation of the Pole, situation of the meridian,
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dian, and variation of the Needle, at any place by the Sunne,
vpon two obseruations, either in fornoone or afternoone,

¶ The eight Chapter.

Of the Pole of the Magnes.

¶ The ninth Chapter.

Of the point Respectiue,

¶ The tenth Chapter.

Of the inconueniences and defects in saylyng, and in description of Countries, caused by the variation of the Compas.

¶ The eleventh Chapter.

Of the Instruments and rules of Nauigation.

¶ The twelfth Chapter.

Of the application of the Variation, to the vse of Nauigation.





Of the Variation of the Cumpas or Magneticall Needle.

Chapter I.



HE Variation of the Needle or Cumpas, is properly the ark of the Horizon contained between the true meridia of any place and the magneticall meridian of the same, and is denominated to bee Easterly or Westerly, according to the position of the magneticall meridian to the Eastwards or Westwards of the true meridian: And may be accompted either from the North parte, or the South parte thereof, but vppon opposit points it hath contrary denominations.

The magneticall meridian is to bee understood a greate circle passyng by the Zenith and the Pole of the Magnes, diuidyng the Horizon into two equall parts crossyng the same at opposit points: which intersections or crossynges, are shewed by the Needle or wiers of the Cumpas touched with the Magnes or the Lodestone.

The Azimuth of the Sun is a great circle, passyng by the Zenith and the true place of the Sun: crossyng the Horizon at right Angles in opposit poinets, and diuidyng the same into two equall parts. And it is said to be giuen When the distance thereof from the true meridian is knowne.

The Azimuths of the Sun vpon equall eleuations in forenoone and afternoone, haue equall distances from the true meridian, so that the middle poinet of the whole difference of any two Azimuths obserued vpon equall eleuations in forenoone and afternoone, is the true meridian.

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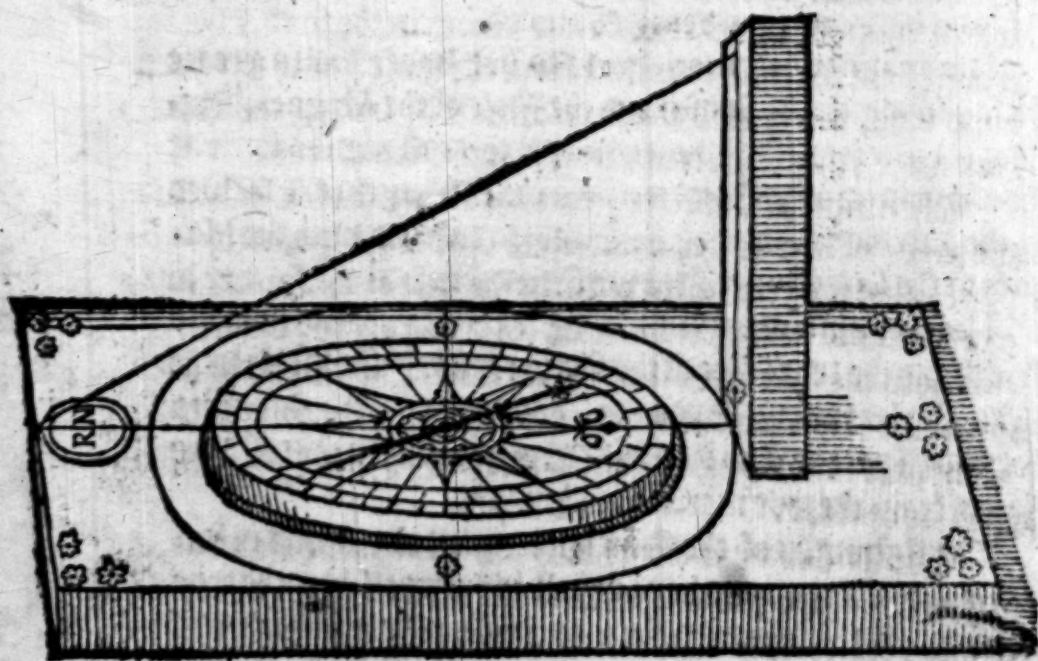
Of the Variation

This difference of Azimuths is found vpon the Instru-
ment of Variation, by addyng together the Variations of the
Sunnes shadowe at equall eleuations in fornoone and after-
noone. The half whereof is the distance of the Azimuths from
the true Meridian: the whiche compared with either of the
same variations of the Sunnes shadowe, the difference shalbe
the variation of the Needle from the true meridian.

Or els subtracting the lesser variation of the Sunnes sha-
dowe, from the greater (at equall eleuations) the halfe of the
remayner shall be the true variation of the Needle from the
meridian.

But the Azimuth of the Sunne beyng otherwise giuen,
and the variation of the shadowe likewise giuen, the difference
betweens them is the variation of the Needle.

The Variation of the Sunnes shadowe I call, the Hori-
zontall distance betweene the Azimuth of the Sunne and the
magneticall circle, whiche are represented in the Instrument
by the shadowe of the line and the Needle.



of the Cumapas.

*The maner how to vse the Instrument
of Variation.*

The second Chapter.



First you must place the Instrument vpon some Stoole, or other thyng that is flat, so as it may stande leuell, and the Plummēt in the Standard which is placed at the North ende of the fixed Flye, may fall perpendicularly with the line in the same Standard.

You must haue regard that in remouing the Instrument to the Sunne as he goeth about, it may alwaies stande leuell as aforesaid.

You are then to consider, that the string that reacheth from the South part of the Instrumēt, to the top of the Standard, is the chiefest string to giue the Sunnes shadow, which must be so directed by turnyng the Instruments South side to the Sunne wards, that the shadowe of the same may fall directly longest vpon the line of South and North in the fixed Flye, for it ought not to crosse or decline from the same line in any part, but if it do, you must seeke to refoyme it by setting the Standard more vpright, or remouyng it at the South end.

Then must you also see, that the string that is fastned to the boope of Brasle that enuironeth the fixed Flye, maie be so placed, that it agree iustly with the shadow of the former line, and the line of South and North in the fixed Flye, in such sort that both the shadowes maie be as it were hidden in the said line of the Flye: which you maie doe aptly, by turnyng the said boope, and remouyng the same line at either side of it, as you shall see cause.

The Instrument beyng duly placed in forme aforesaid, it differeth nothyng from the Cumapas of Variation, but onely in this point, that whereas the Flye of the Cumapas of Variation, is so turned by vertue of the Magneticall wiers, that

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the North point thereof doeth shew the Pole of the Magnes
or line of Variation: In this Instrument, the North point of
the Needle doeth supply that, whiche the North point of the
Cumpas should doe. And the North point of the Flye which
is fixed in the bottome of the Instrument, doth alwaies an-
swere to the shadowe that the Sunne giveth.

*How to finde the variation of the Needle or Cumpas
at any place, the elevation of the Pole, and situation
of the meridian unknowne.*

The third Chapter.



When you would obserue the variation in
any place, you must begin in y^e fornoone,
the sooner, the better, and the more effec-
tuall make your obseruations be, do thus.

Take your Astralabe and obserue du-
ly the height of the Sūne, for your more
ease it shall bee best for you to note the
same, when it agreeth to be iust vppon a degree, without any
consideration of minuts or fractions, and at the instant of the
same height, turne your Instrument to the Sunne, so as the
shadowe of the lines maie fall iustly vppon the line of South
and North in the fixed Flye.

Then, when the Needle doeth stande, looke directly ouer
the North point of the Needle, what degree and fraction, if
there be any, doth answer vnto the same in the fixed Flye,
that is to saie, how many degrees it is from the North of the
fixed Flye, which you shall note diligently, and may saie, that
so many degrees &c. is the variation of the Sunnes shadowe
from the North, as the North point of the Flye is from the
North point of the Needle, either Eastwardes or West-
wardes as you shall finde the same. Thus maie you obserue
diuers tymes, vpon severall degrees of the Sunnes elevati-
on. And like as you doe in the fornoone, so must you also ob-
serue

of the Cumpas.

serue the Sunnes eleuation in the afternoone, vpon the same degree of height, and with the same side of the Astrolabe and Index turned towards the Sunne, as it was in the fornoone, (for auoyding of error that maie bee in the Instrument) noting at euery height what you finde the variation. And when the Sunne commeth to the meridian, it shall be good that you exactly obserue his eleuation vpon the same, for knowyng the true Latitude of the place: all whiche you shall set downe in forme followyng.

¶ Example.

In Limehouse the sixteenth of
October. Anno, 1580.

Fornoone.			Afternoone.		
Eleuation of the Sunne.	Variation of the Shadow from the North of the Needle to the Westwards.		Eleuation of the Sunne.	Variation of the Shadow from the North of the Needle to the Eastwards.	Variation of the Needle from the Pole or Axis.
Deg.	Degr.	Min.	Deg.	D. M.	D. M.
17	52	35	17	30 0	11 17 $\frac{2}{3}$
18	50	8	18	27 45	11 11 $\frac{1}{3}$
19	47	30	19	24 30	11 30
20	45	0	20	22 15	11 22 $\frac{1}{3}$
21	42	15	21	19 30	11 22 $\frac{1}{3}$
22	38	0	22	15 30	11 15
23	34	40	23	12 0	11 20
24	29	35	24	7 0	11 17
25	22	20	25	Fró N. to w. 0.8	11 14

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Of the Variation

The elevation of the Sunne vppon the meridian 25.d.58'. the declination 12.d.30'. whiche I adde to the elevation, because the Sunne hath South declination, and thereof amounteth 38.d.28'. the elevation of the Equinoctiall, the whiche I subtraſt from 90.d. the rest is 51.d.32'. the elevation of the Pole Artik.

Now are you to consider, that out of the greater variation of Shadow vpon any degree of the Sunnes elevation, is to be taken the lesser of the same degrees elevation, whether it bee in the forenoone or afternoone, (except the same variations be bothe one waie from the North of the Needle, whiche then are to be added) the halfe of the remayner is the variation of the Needle or Cumpas from the Pole or true meridian.

In the former obseruations, I do finde the greatest variation in the forenoone, for, at 17.d. elevation, the variation is 52.d.35'. from North to West: And at the same elevation in the afternoone, I finde the variation to be but 30.d.0'. frō North to East. I take the lesser out of the greater and finde remayning 22.d.35'. the half thereof is 11.d.17. $\frac{1}{2}$. So much I say is the Pole Artik, and true meridian line that passeth to the Pole by our Zenith at London, to the Westwardes of the North that the Needle sheweth. And therefore the Needle or Cumpas varieth from the true North 11.d.17. $\frac{1}{2}$. to the Eastwardes.

Also at 25.d. elevation in the forenoone the variation is 22.d.20'. from North to West: at the same elevation in the afternoone the variation is 0.d.8'. from North to West. Now because the variations are both one way, (that is to the Westwardes) I adde them together (and so ought you to doe as often as you finde the variations so to agree) and I finde that they amount to 22.d.28'. the half thereof is 11.d.14'. which is the variation.

The variations of the Needle or Cumpas by the former obseruations, are set out towardes the right hand against every degrees elevation, and conferrynge them all together, I do finde the true variation of the Needle or Cumpas at Lynce-house

of the Cumpas.

house to be about $11.d.\frac{1}{2}$. or $11.d.\frac{1}{3}$. whiche is a poinct of the Cumpas iust or little moze. So that in a Cumpas whose wires are set directly vnder the flowze de Luce, the North and by West, and South and by East poincts doe shewe the true meridian.

The eleuation of the Pole and place of the Sunne giuen how vppon the Globe, to finde the variation of the Needle by any one obseruation, either in fornoone or afternoone.

The fourth Chapter.



In the former declaration, the onely way to try the variation, is by comparynge of the seuerall correspondent obseruations of the Sunnes eleuation in the fornoone, with those of the afternoone, so that if the Sunne should bee obscured, or by any other occasion like obseruation can not be made in the afternoone, then the former rule giueth not the desired purpose. Therefore I thought good to shewe, how by any one obseruation in the fore or afternoone, the eleuation of the Pole and place of the Sunne giuen, you maie knowe the true meridian and the variation of the Needle from the same in any place, whiche thing maie be done and aptly demonstrated vpon the Globe, but mooste exactly calculated by the Table of Sines.

To finde out the variation vpon the Globe, you must first set your Globe to stande dewly accordyng to the eleuation of the Pole at the place proposed. Then seeke in the Ephemerides for the true place of the Sunne that daie, and note it with some small prick in the ecliptik of the Globe. And placynge the Quadrant of Altitude or moueable verticall, at the verticall poinct or Zenith, take the eleuation of the Sunne obserued by the Astrolabe or other Instrument at the tyme proposed, and
note

Of the Variation

note it iustly vpon the same quadrant of altitude. Then turne your Globe and quadrant towardes that part of the Horizon that the Sunne was in at the tyme of the obseruation, till the prick you made for the place of the Sunne in the ecliptick, concur and agree iustly with the eleuation marked in the said quadrant of altitude. So shall you see the quadrant shewe you vpon the Horizon, the Azimuth and distance of the Sunne from the true meridian of that place, whiche you shall compare with the variation obserued vpon the Instrument at that instant of the Sunnes eleuation, And if they agree and concur iust, then shall you bee in the true and common meridian, whiche sheweth the Pole of the worlde and Pole of the Magnes or Lodestone: But if they differ, you shall subtrakt the lesser from the greater, the remayner sheweth the variation. And if the variation vpon the Instrument be greater then the true distance of the Azimuth from the meridian founde vpon the Globe, the same surplus is to be accompted for variation, vpon the contrary side of the meridian: if it bee lesse, it is to be accompted on the same side of the meridian that the variation is taken, whether it bee in the forenoone or afternoone. This precept needeth no further demonstration, then the Instrument it self, the Globe I meane.

But for example of the worke, I take the first obseruation, in the former Chapter specified, made at Lynnhouse the sixteenth of October. 1580. in the forenoone, which is 17.d. eleuation, and variation 52.d. 35'. from North to West.

First I set my Globe at 51.d. 32'. for the eleuation of the Pole. Secondly I take the place of the Sunne 2.d. 55'. m. and note it vpon the Ecliptick. Thirdly I note vpon the quadrant of altitude, the eleuation of the Sunne 17.d. This done, I moue the quadrant of altitude towardes the East of the Horizon, and turne the Globe till the prick in the Eclipticke for the place of the Sunne, doe agree iustly, with the eleuation noted vpon the quadrant of altitude, and finde the true Azimuth shewed by the said quadrant vpon the Horizon to be next, about 41.°, from the meridian. And conferring the same with

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with the variation founde vppon the Instrument 52.d.35'. I find the difference 11.d.15'. And because the obseruation is noted to be in the fornoone frō the North to the West, or South to the East, and the variation vppon the Instrument greater then the Azimuth founde on the Globe, I accompt the same from the North to the East, or from the South to the West. So I conclude the variation at Lymehouse to be about 11, $\frac{1}{4}$, from North to East, or South to West.

¶ How to finde the variation by Arithmeticall calculation vpon any one obseruation in the fornoone or afternoone, the Latitude of the place, and declination of the Sunne beyng giuen.

The fift Chapter.



THE summe of the worke, is to finde the arke of the Horizon, betweene the meridian and the Azimuth of the Sunne at the time of the obseruation, whiche beyng compared with the variation founde in the Instrument, the difference is the variation of the Needle.

For attaynyng of the same arke. First it is necessarie to haue the arke of the Equinoctiall betweene the Sunne at the tyme of the obseruation, and the meridian, which arke is thus found.

Multiply the line of the Sunnes meridian altitude for the daie proposed, by the whole line, the product diuide by the line of the eleuation of the Equinoctiall (or the complement of the Latitude) the quotient is the versed line or shaft of the semidiurnall arke, whiche you shall note for the first number.

Then againe multiplie the line of the Sunnes eleuation at the tyme of the obseruation, by the whole line, and the product diuide by the line of the eleuation of the Equinoctiall, the quotient subtract from the number you first noted, the rest is the versed line of the arke of the distance betwene the Sunne and the meridian in the parallell that it is in for the tyme pro-

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posed,

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posed, in suche partes as the Semidiameter of the Equinoctiall is the whole line: but it is necessarie before you applie it any furder, to reduce it into suche parts as the Semidiameter of the parallell is the whole line, whiche you maie doe thus: Multiplie this remainer by the whole line, the product diuide by the line of the complement of the declination (which is the Semidiameter of the parallell) the quotient is the versed sine in his proportionall parts.

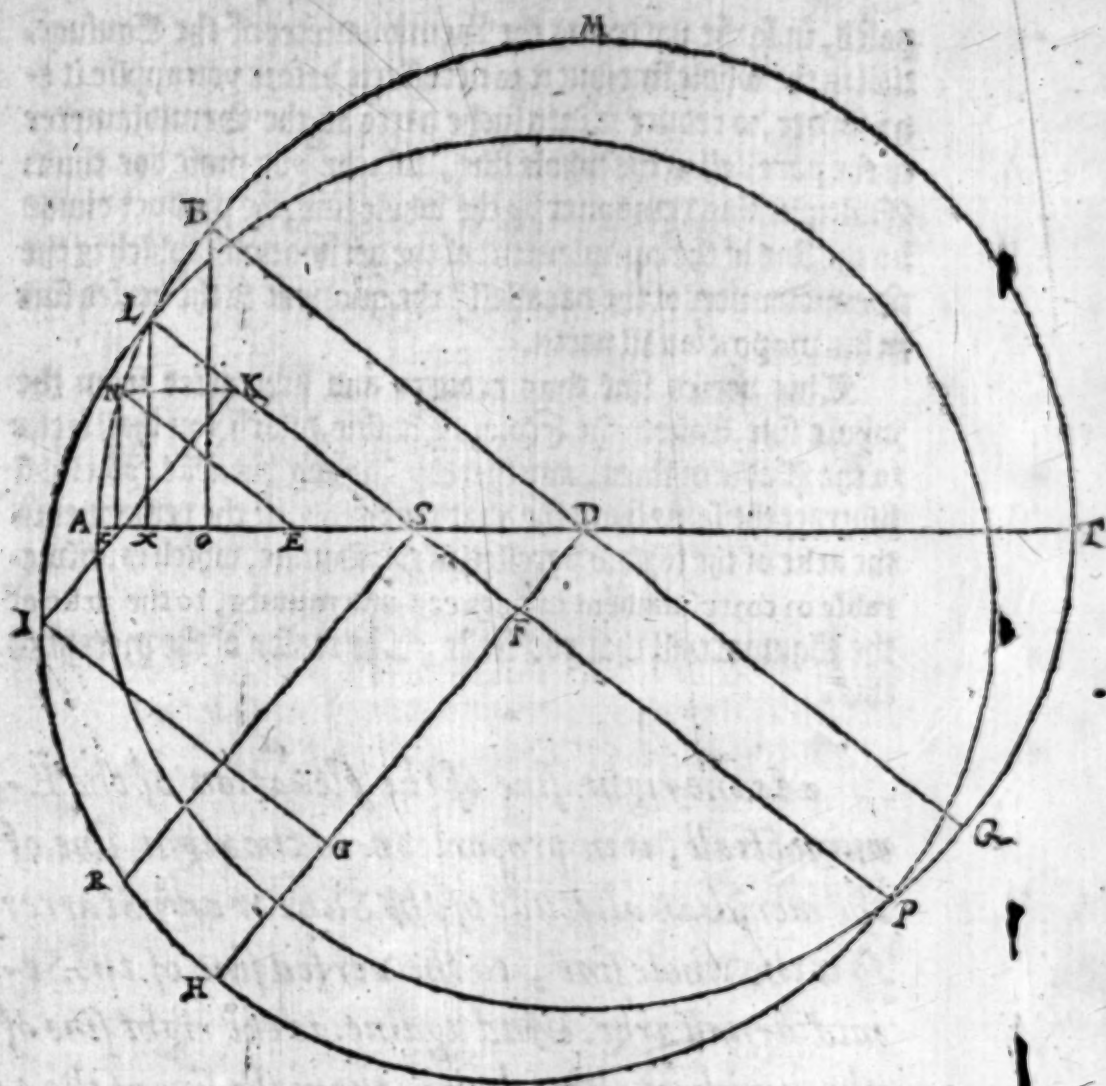
This versed sine thus reduced and subtracted from the whole line, leaueth the second right sine, which you shall seeke in the Table of lines, and thereby finding his arke, you shall subtract the same from the quadrant or 90. d. the remainer is the arke of the foresaid parallell of the Sunne, which is answerable or correspondent in degrees and minuts, to the arke of the Equinoctiall that you seeke. The reason of the precept is this.

As the right sine of the eleuation of the Equinoctiall, is in proportion to the right sine of the meridian altitude of the Sunne or any Starre: so is the whole sine, to the versed sine of the Semidiurnall arke. And againe, as the right sine of the meridian altitude, is to the right sine of the eleuation of the Sunne or Starre at the tyme of the obseruation: So is the versed sine of the Semidiurnall arke of the same, to the excesse or difference betweene the same versed sine and the versed sine of the distance from the meridian.

For the better understanding of the premisses, I haue set downe this figure following, and wishe the Reader to consider of the same with the 4. Pro. of the 6. of Euclide.

Let

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L Et AMT . be the meridian circle. BDQ . the common section of the meridian and Equinoctiall their playnes, whiche is also the diameter of both circles. ADT . the plaine of the Horizon. LHP . the parallell of the Sunne, whiche is described vpon the centre F . at the distance FL . whiche is the sine of the complement of the declination. AB . the arke of the eleuation of the Equinoctiall. BO . the first right sine thereof. AL . the arke of the meridian altitude. LX . the sine thereof. AN . the arke of the Sunnes eleuation

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elevation

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elevation at the tyme of the obseruation. N C. the sine thereof. B D. the whole sine in respect of the former arkes and fines. L R. the Semidiurnall ark of the parallell. R S. the first right sine thereof. S L. the versed sine of the same. L I. the ark of the Sunnes distance from the meridian. I K. the first right sine thereof. I G. the second right sine, which is equall to K F. K L. the versed sine. N E. which is equall to K S. the differēce of the 2. versed fines L S. and L K. L F. the whole sine in respect of the arks and fines of the parallel.

Now as B O. is to L X. so is B D. to L S. And as L X. to N C. so is L S. to N E. Or els thus, as B O. to N C. so is B D. to N E.

Example.

The 16. October, 1580. in Lymehouse.

The elevation of the Pole Artik 51.d.32'. The declination of che Sunne 12.d.30'. The elevation of the Sunne obserued in the fornoone 17.d.0'. The variation of the shadow upon the Instrument 52.d.35'. from North to West.

38.28'.	90.0'.	25.58'.	
BO.	BD.	LX.	LS.
If. 62205. gine. 100000. — then. 43784. giuesh. 70386.			
38.28'.	90.0'.	17.0'.	
BO.	BD.	NC.	NE.
Again if. 62205. gine. 100000. 29237. shall gine. 47001.			

Now out of, L S. — 70386.

take. N E. — 47001.

Rest. L K. — 23385.

Then if L F. 97629. the sine of 77.d.30'. the complement of the declination, gine L F. 100000. then L K. 23385. giueh L K. 23952. the versed sine of the arke I L. in his dew partes.

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The same subtracted from $L.F. 100000$. the whole sine, leueth $K.F.$ or $I.G. 76048$. the second right sine of the same ark, which is the first right sine of the arke $I.H.$ whiche arke you shall finde in the table of sines to be $49.d.30'.24''$. the complement whereof to the quadrant is $40.d.29'.36''$. the arke $I.L.$ of the parallell betweene the Sunne and the meridian, whose correspondent ark in the Equinoctiall, is the arke that was sought.

Now hauing this done of the Equinoctiall, you must worke

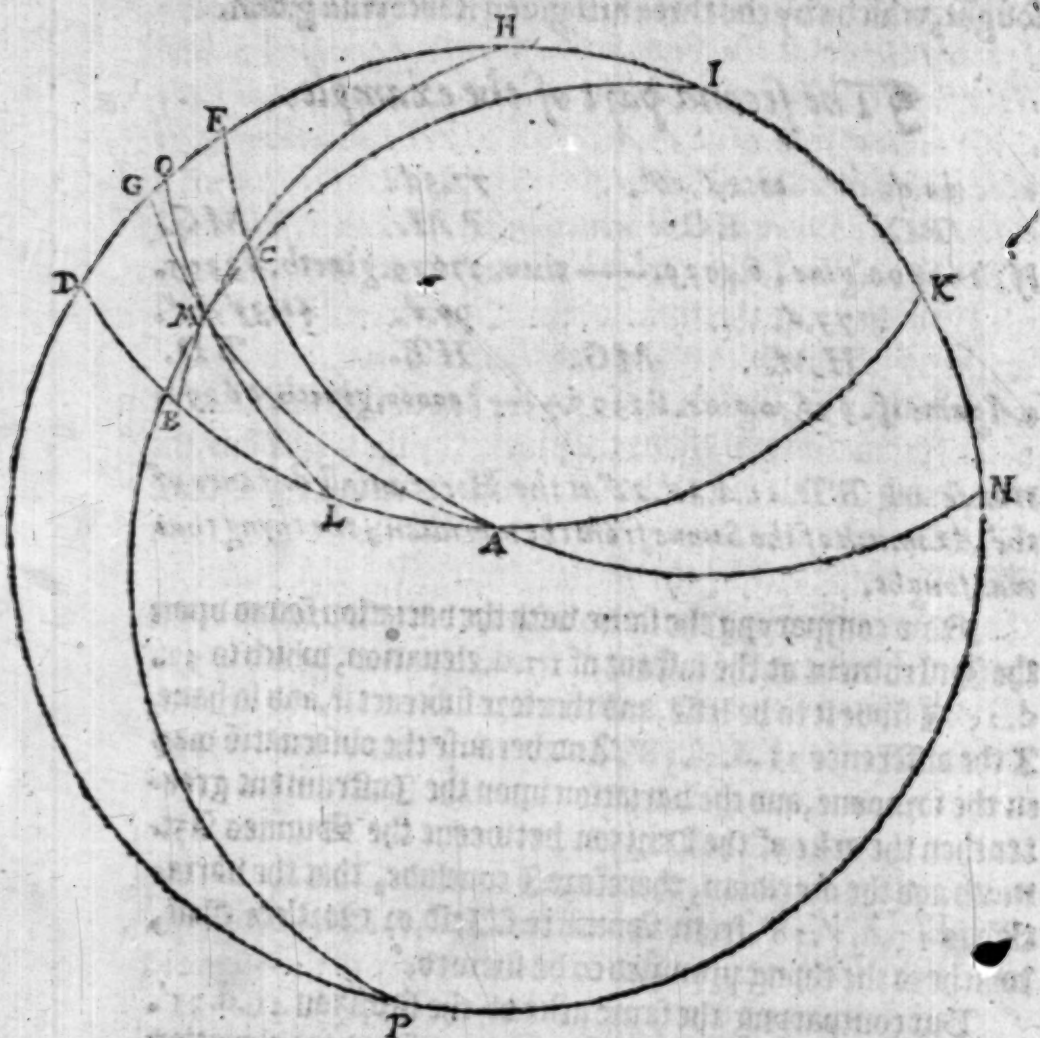
the same line thereof, by the sine of the complement of the declination, and diuide the product by the whole sine, the quotient is the sine of an arke contayned betweene the Sunne and the meridian, makynge right angles with the meridian. This sine multiply by the whole sine; the product diuide by the sine of the complement of the Sunnes eleuation at the tyme of the obseruation, the quotient shalbe the sine of the ark of the Horizon contained between the Azimuth of the Sunne and the meridian, whiche is the arke that was proposed to be found.

L Et $DHNP.$ be the meridian. $DAK.$ the Horizon. $EAN.$ the Equinoctiall. $M.$ the place of the Sunne in the heauen at the tyme of the obseruation. $LMO.$ the parallell. $HMB.$ the Azimuth or verticall circle passing by the Sunne. $AMG.$ a greate circle imagined to passe by the Sunne, & to crosse the meridian at right angles. $IMP.$ a greate circle passyng by the Poles of the worlde, and place of the Sunne at the tyme of the obseruation, commonly called the citcle of houres, or circle of declination. $CM.$ the South declination of the Sunne. $MC.$ the complement thereof to the quadrant. $MB.$ the ark between the Sunne and the Equinoctiall of the former imagined circle. $AMG.$ the ark of the Sunnes parallell. $EC.$ the correspondent ark of the Equinoctiall, which are giuen in the former work. $MB.$ the eleuation of the Sunne at the tyme of the obserua-

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tion. MH . the complement thereof. BD . the ark of the Horizon intercepted between the Azimuth and the meridian, which is the thing required to be found.

In this figure the Reader is to consider the maner of the sphericall triangles, and to compare the sides of their sides, according to the doctrine of Copernicus. in the 14. Chapter of his first booke, and of Regiomontanus. his 25. and 27. propositions of his 4. booke of triangles.

As PC . is to CE . so is PM . to MG . but 3. of them are given, therefore the fourth shall be known.

And as HM . is to MG . so is HB . to BD , the arke that is sought,

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sought, which by the three first giuen is likewise giuen.

The second part of the example.

90.d.	40.29'.36".	77.30.	
P.C.	E.C.	P.M.	M.G.

If, 100000.gine, 64935. — then, 97629.gineth, 63395.

73.d.		90.d.	41.31'.22".
H.M.	M.G.	H.B.	B.D.

Againe if, 956.gine, 63395. — 100000.gineth, 66291.

Whose B.D. 41.d. 31'. 22". is the Horizontall distance of the mouth of the Sunne from the meridian, the thyng that m^oghr.

Now comparvng the same with the variation found vpon the Instrument at the instant of 17.d. eleuation, which is 52.d. 35'. I finde it to be lesse, and therfore subtrakt it, and so haue I the difference 11.d. 3'. 38". And because the obseruatiō was in the fornoone, and the variation vpon the Instrument greater then the arke of the Horizon betweene the Sunnes Azimuth and the meridian, therfore I conclude, that the variation is 11.d. 3'. 38". from South to West, or North to East, whiche is the thyng promised to be shewed.

But comparvng the same arke of the Horizon 41.d. 31'. 22". with the variation founde at the correspondēt eleuation in the afternoone, which is 30.d. 0'. I subtract the lesser from the greater, and finde the excesse 11.d. 31'. 22". whiche should be the variation. And because the variation founde vpon the Instrument is lesse then the arke of the Azimuth vpon the Horizon, I accompt the variation on the same side of the meridian, whiche is from South to West, or North to East.

This varietie betweene the obseruation made in the fornoone, and that in the afternoone, proceedeth either of the imperfection of the Instrument, or negligence of the obseruer. For in the rule there can bee no error, beynge grounded vpon Geometricall demonstration, then whiche nothyng can bee more

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more certaine.

The former preceptes and examples doe serue when the Sunne doth decline frō the Equinoctiall either Northwardes or Southwardes. But if the Sunne be in the Equinoctiall, then the maner of the workyng is more easie and brief. For if you multiplie the sine of the Sunnes eleuation at the tyme of obseruation, by the whole sine, and diuide the product by the sine of the eleuation of the Equinoctiall, whiche is the meridian altitude, the quotient giueth the seconde right sine of the distance of the Sunne frō the meridian, whiche is the first right sine of the complement of the same arke: And entryng the table of sines with it, you shall finde his arke, whiche if you subtract frō the quadrant or 90.d. leaueth the arke of the distance of the Sunne from the meridian. And hauyng the same work thus. If the sine of the complement of the eleuation of the Sun at the tyme of the obseruation, giue the sine of the forsaide arke of distance, what shall the whole sine giue. Multiplie and diuide, the quotient shalbe the sine of the ark of the Horizon contained betweene the Azimuth of the Sunne and the meridian. Which arke being compared with the variation of the Instrument in maner as before is shewed, giueth the variation required.

But the Sunne beyng in the Equinoctiall, if the place where the obseruation is made, bee likewise vnder the same circle; then is the variation most easely obserued. for that the Equinoctiall is the Azimuth of East and West, therfore turning your Instrument onely to receiue the shadowe of the Sunne, and looking then to the North point of the Needle, if you finde the same to aunswere to the quadrant or 90.d. you shall be in the meridian of the Magnes, whiche passeth by the Poles of the world, but if it doe differ from 90.d. the same difference is the variation of the Needle.

But admittynge the obseruer to be vnder the Equinoctiall, and the Sunne to haue declination, then the proportion of the sine of the complement of the eleuation at the tyme of the obseruation, vnto the sine of the declination, shalbe suche, as the whole

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whole line, is to the line of the arke of the Horizon included betweene the Azimuth of East and West, which is the Equinoctiall it self, and the Azimuth of the Sunne for the tyme of the obseruation, the complement whereof giueth the true meridian, whiche complement you maie compare with the variation shewed vpon the Instrument, the difference is the variation.

Diuers other cases might bee proposed, and rules giuen for them, whiche for breuitie I omit.

But one thpyng I thought good to admonishe you by the waie, that whereas I haue shewed in the first part of this proposition the maner to finde the two versed lines, the one of the Semidiurnall arke, the other of the arke of the distance of the Sunne from the meridian. By the first, the Semidiurnall arke being found and reduced into houres and minuts of time, is shewed the iust quantitie of the daie. And by the arke of the other likewise reduced, the houre of the day, or the tyme contained betweene the noonsteed and the instant of the obseruation. As in the same example. The versed line of the Semidiurnall ark LS. is giuen 70386. in suche parts as the Semidiameter of the Equinoctiall BD. is 100000. therefore I reduce the same into such parts as the Semidiameter of the parallel LF. is 100000, and finde it to be 72095. which subtracted from the whole line LF. 100000. there resteth SF. 27905. whiche is the second right line of the Semidiurnall ark LR. and the right line of RH. 16.d. 12'. whiche is the complement of the Semidiurnall Ark LR. wherefoze subtractyng it from the quadrant LH. or 90.d. resteth 73.d. 48'. the Semidiurnall ark LR. the same reduced into partes of tyme allowyng 15.d. for an houre 15'. for a minut, and 15". for a seconde of tyme, and for euery degree 4. minuts of tyme, for euery minut 4". and for euery second 4". &c. I finde the time of that ark from the point ascendent, to the meridian, whiche is halfe the day, to bee 4. houres 55'. 12". and consequently the whole day beyng the 16. of October aboue written, to be 9. houres 50'. 24". long.

This

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This example maie serue for a generall precedent, whiles the Equinoctiall is betweene the Sunne & the eleuated Pole, but if the Sunne be between the eleuated Pole and the Equinoctiall, then will the versed sine fall out to be greater then the whole sine, and the Semidiurnall arke to excede a quadrant. Wherefore haupng reduced the same into his proportionall parts, as before is shewed, subtract from it the whole sine, the surplus is the sine of the excesse of the Semidiurnall arke above a quadrant, whiche bepng added to the quadrant, giueth the Semidiurnall arke.

By the other versed sine of the distance of the Sunne from the meridian, which is L K. 23952. in such parts as the whole sine of Semidiameter L F. is 100000. subtracted from the whole sine, is giuen KF. 76048. the second right sine of the same ark of distance, and the first right sine of 49. d. 30'. 24". which is the complement of the ark of the Sunnes distance from the meridian: therefore subtractyng the same from 90. d. resteth 40. d. 29'. 36". the arke of the distance betweene the Sunne and the meridian, which bepng reduced into partes of time as before, giueth 2. houres 41'. 58". and the same (because it is in the fornoone) deducted from 12. houres the noonsteed, resteth 9. houres 18'. 2". the iust instant of the tyme of the day.

But if this versed sine be found to be greater the whole sine (as it maie when the Sunne is betweene the Equinoctiall and the eleuated Pole, and before the houre of sixe in the mornypng and after the houre of sixe in the euenypng) then both the arke of distance consequently excede a quadrant, the sine of this excesse is the surplus of the versed sine above the whole sine. Whose arke added to the quadrant giueth the arke of the Sunnes distance from the meridian, and reducyng the same into partes of tyme, is giuen the instant of tyme of the obseruation.

As by this meanes (the eleuation of the Sunne being precisely obserued and Latitude knowen), the instant of time of daye is giuen more exactly, then by any Clock, Diall or other Instrument. So if there might be had a portable Clocke that would

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would continue true the space of 40. or 50. houres together (if longer tyme the better) then might the difference of longitude of any two places of known Latitudes, whiche conveniently may be trauelled within that time, be also most exactly giuen. And in this sort traueilling and obseruing from place to place, might the longitudes of any Countrey be perfectly described.

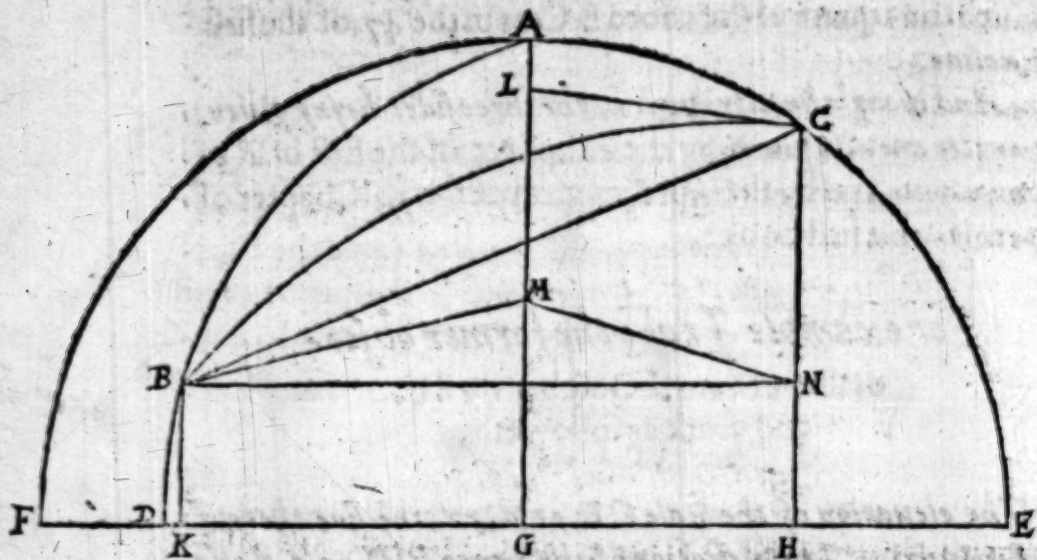
¶ An other way most generall, how to finde the Variation by one obseruation either in the fornoone or afternoone, the eleuation of the Pole and declination of the Sunne beyng giuen.

The sixt Chapter.



FOR the accomplishing of this proposition, you are to imagine a sphericall triangle vppon the superficies of the Globe, whose sides must be. First the portion or arke of the meridian betweene your Zenith and the Pole, whiche is the complement of the latitude. The second the arke of the verticall circle containned betweene your Zenith and the Sunne, which is the complement of the Sunnes eleuation at the tyme of the obseruation. The third side is an arke of the circle of declination comprehended betweene the Sunne and the eleuated Pole, this arke is found by adding, or subtracting, the declination of the Sunne, to or from, the quadrant or 90. d. whiche must be done with this consideration, that if you be on the same side of the Equinoctiall that the Sunne is, you are to subtract the declination from the quadrant. If on the other side, to add it to the same, so haue you the three sides of the sphericall triangle giuen. Then the substance of the work consisteth in finding the quantitie of the angle of the same triangle at the Zenith, for the complement thereof to the Semicircle or two right angles, is the Horizontall distance of the Sunnes Azimuth from the meridian, which beyng compared with the variation of the Sunnes shadowe vppon the Instrument, giueth the thyng required.

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L Et FACE. be the meridian, wherein A. the Zenith, C. the Pole. AD. the verticall circle or Azimuth of the Sunne passing by B. the place of the Sunne at the tyme of the obsetuation. BD. the eleuatiō of the Sunne. BA. the complement of the eleuation. AC. the complement of the latitude. BC. the ark of the circle of declination, or the chord of the same ark. FGE. the plaine of the Horizō.

Now from the three angles of the triangle ABC , let fall 3. perpendicular lines to the plane of the Horiz^o AG , CH , and BK , and by the 6. of the 11. of *Euclide*, these three lines shall be parallelles.

Then let fall a perpendicular line from C. vppon A G. in the point L. from B. an other perpendicular vppon the same line A G. at the point M. And from the same point M. erect a perpendicular line to N. which shalbe parallell and equall to L C. Then ioyn B. and N. together. So haue you a right-lined triangle. B M N, whose angle at M. is equall to the angle A. of the sphericall triangle A B C. By the 4. definition of the 11. of *Euclide*, for the like reason is of obtuse angles as of acute or sharp. And the sides therof B M. and M N are giuen B M. the sine of B A. and M N. equall to L C. the sine of C A.

And

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And the third side BN. is found by subtracting the square of NC. from the square of the chord BC, as in the 47. of the first of *Euclide*.

And in rightlined triangles, the three sides being given, the angles are also given, by the 44. 45. &c. of the first of *Regiomontanus*, and by the 7. proposition of the 13. Chapter of *Copernicus* his first booke.

For example I take the former obser-
uation of the 16. October 1580.
and work as followeth.

The elevation of the Pole CE. 51. d. 32'. the sine thereof CH. 78297. The elevation of the Sunne BD. 17. d. 0'. the sine thereof BK. 29237. The arke BC. 102. d. 30'. the chord thereof BC. 155976. The complement of the elevation of the Sunne BA. 73. d. 0'. the sine thereof BM. 95630. The complement of the latitude AC. 38. d. 28'. the sine thereof LC. 62205. equall to MN. Now out of CH. 78297. subtract NH. equall to BK. 29237. Rest NC. 49060.

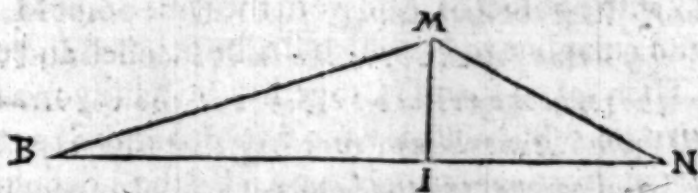
Then out of the chord BC squared, ——— 24528512576.

Take the square of NC. ————— 2406883600.

Rest the square of BN. ————— 21921628976.

The roote thereof is. 148059. the side BN.

So are the three sides of the triangle given. $\left\{ \begin{array}{l} BN. 148059. \\ MN. 62205. \\ BM. 95630. \end{array} \right.$



Now to finde the angle M. I subtract from the square of BM. the bigger side, whiche is. 9145096900. the square of
D. iij. MN.

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MN. the lesser side, which is. 3869462025. Rest 5275634875. which divided by the base *BN*. 148059. giveth 35631. which number I take out of the said base rest, 112428. the half thereof. 56214. is *IN*. the lesser case or shorter parte of the base divided by the perpendicular line *MI*. falling upon the same from the obtuse angle *M*. whiche subtracted from the whole base *BN*. 148059. leaveth *IB*. 91845. the greater case or longer part thereof.

Now it is manifest that these two cases or parts of the base *BI* and *IN*. are the sines of the two sharpe angles *IMB*. and *NMI*. made of the obtuse angle *M*. by the perpendicular falling from the same angle to the base, and the arcs of them joyued together, are the quantitie of the obtuse angle *NMB*.

Therefore to reduce them to the numbers of the sines, first for the greater case *BI*. making *BM*. the whole sine, say.

<i>BM</i> .	<i>BM</i> .	<i>BI</i> .	<i>BI</i> .
If. 95630. sine. 100000.—		then shall. 91845. sine. 96042.	

The ark thereof is 73. d. 49'. 38". Againe for the lesser case, making *MN*. the whole sine, say.

<i>MN</i> .	<i>MN</i> .	<i>IN</i> .	<i>IN</i> .
If. 62205. sine. 100000.—		then. 56214. sine. 90376.	

Whose ark is 64. d. 38'. 45". And adding these two arcs together they give 138 d. 28'. 23". the ark or quantitie of the obtuse angle *NMB*. equall to the sphericall angle *BAC*. And deducting it from the Semicircle 180. d. there resteth 41. d. 31'. 37". the angle *FAD*. the Horizontall distance of the Sunnes Azimuth from the meridian, & subtracting that from 52. d. 35' the variation found vpon the Instruient from North to West in the fornoone, resteth 11. d. 3'. 23". the variation of the Needle from the meridian, the thying that was proposed to be found. And comparing the same with the afternoones observation, you shall finde it 11. d. 31'. 37". the cause of this difference I have declared in the former Chapter.

If the Reader be delighted with varietie of demonstrati-

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On of this matter, let him peruse the 34. proposition of the 4. of Regiomontanus, and the 13. proposition of the 14. Chapter of the first booke of Copernicus.

But whereas you see this calculation to differ from the former in some odde seconds, the reason thereof is not as it might bee taken the different nature of the rules, but in working thereof, omitting the fractions in the diuisions, and neglecting the proportionall parts of the lines and arcs.

In these exāples I haue vsed y abridged table of 100000. the whole line, which though it giue some ease in the working, yet it is not so exact as that of 10000000. of Erasmus Reinholdus. Unto the which, with his Canon secundus answerable to the same, if the third Canon of the Hypothenusæ were annexed, we should haue an entire table for the doctrine of triangles, that might worthely bee called The table of tables. Whiche thyng though Georgius Ioachimus Rheticus, haue well begun and framed it orderly frō ten minuts to ten: yet is it left very rawly for suche as desire the exact truth of thynges. I haue therefore for myne owne ease and vse, calculated the complement of this table, and almost ended it, for the whole quadrant from minut to minut: whiche if in the meane tyme before I haue finished, I shall not finde it extant by any other, I will publishe it for the commeditie of all suche as shall haue occasion to vse the same for Nauigation and Cosinography.

¶ To finde the eleuation of the Pole, Situation of the meridian, and Variatiō of the Needle at any place by the Sunne, vpon twoo obseruations either in forenoone or afternoone.

The seuenth Chapter.



Whereas in the three last Chapters, the groundes of the calculations consist in the eleuation of the Pole to be giuen, which thyng to knowe is no lesse difficult,

Of the Variation

cult, then the cheef matter that is by them required. For the common precepts, whiche as yet haue theefly been giuen for the finding thereof, depende onely vppon the obseruation of the meridian altitude of the Sunne or Starres, or els vppon certaine false and grosse rules of the guardes and Pole Starre. Therefore I haue thought good, that as I haue shewed the waie to know the variatiō vpon any one obseruation, either in forenoone or afternoone, the latitude of the place presupposed: so likewise, vpon two obseruations by the Sunne, either in forenoone or afternoone, to sette doune the waie and maner how to finde the eleuation of the Pole, situation of the meridian, and variation of the Needle in any place by the Globe.

But this you must alwaies regard, that your two obseruations maie haue conuenient distance of tyme betweene them, the greater the better: So as the higher eleuation bee not taken nere the meridian, the lower eleuation the nerer it is taken to the Azimuth of East or West, or to the Horizon, the better, with which eleuations, you are to note the difference of the Sunnes Azimuths or variations founde by the shadowe vppon the Instrument exactly, for without that, the eleuations onely are in vaine.

First it is requisite, that your Globe be so fitted, that the meridian circle and the Horizon doe crosse eche other at right angles, and diuide them selues equally into Semicircles. And also that the quadrant of altitude (or moueable verticall) bee placed dully vpon the meridian circle at the Zenith, so as being turned circularly, it may touche the Horizon equally in euery part. These thinges beyng dully considered, there needeth not any further regard to bee had for placynge of the Globe, onely this you may respect in setting the Pole at aduentures aboue the Horizon betweene it and the Zenith, that the meridian circle may cut the Horizon in iust degrees, so may your quadrant of altitude be placed at your Zenith iustly vpon a degree also.

Then must you fasten your Globe to the Horizon, so as it may remaine immoueable, but in fastnyng the same you must regard that you force it not from one side of the Horizon to an other

of the *Cumpas.*

other, but that it rest equidistant in the same. And haupng your Globe thus disposed, it is ready for you to apply your obseruations vpon, which you shall thus doe.

First, take your highest eleuation, and note it vpon your quadrant of altitude, and place the ende of the saied quadrant vpon the Horizon at 10. 15. or 20. d. frō the meridian circle, (but the nerer you set the same to the meridian, the more conueniently, without impechement, will your triall bee made.) Then giue a picke vpon the Globe in the Azimuth, that the quadrant sheweth at the degree of the eleuation, noted vpon the quadrant, then againe note the lesser eleuation vpon the quadrant of altitude, and remoue the same vpon the Horizon (from that place where it was first fixed, towards the Azimuth of East or West, whiche shalbe nerest the same) so many degrees as you finde the difference of Azimuthes betwene the twoo eleuations by the shadowe of the Summe, vpon the instrument of Variation, and staipng your quadrant of altitude vpon that point of the Horizon: note also your lesser eleuation in the same Azimuth vpon your Globe. This doen you must haue a paire of Calliper compasses, suche as maie conueniently reche to $113. d. \frac{1}{2}$. of the Equinoctiall of your Globe, (whiche is a quadrant, and the greatest declination of the Summe) then you must consider whiche of the Poles of the worlde is eleuated aboue your Horizon, and whether your declination bee towards, or from that Pole, that is to saie, whether the Summe be betwene the eleuated Pole and the Equinoctiall, or the Equinoctiall betwene the Summe and the Pole. If the Summe bee betwene the Pole and the Equinoctiall, then are you to subtracte the declination from 90. d. If the Equinoctiall bee betwene the Summe and the Pole, you must adde the declination to 90. d. And take the same remainyng or collected number of degrees &c. with your compasses vpon the Equinoctiall. And sett the one ende of your compasse at the picke made vpon your Globe, for the highest obseruation, and with the other ende describe an arke or peece of a circle, vpon the same side of the meridian that your picke

Of the Variation

is on, from the meridian to the Horizon. Then againe with your compasse vnaltered, setting the one foote in the picke for the lowest obseruation, describe an other peece of a like circle crossing the former. The point of the intersection, or crossing of these two circles, is the eleuated Pole, to the whiche if you remoue the quadrant of altitude, you shall finde what the eleuation thereof is. And the pointe that the same quadrant sheweth vpon the Horizon, is the intersection of the meridian and the Horizon, the Horizontall distance betweene this intersection, and the Azimuth of the lesser obseruation, subtracted from the semicircle, or 180.d. leueth the Horizontall distance of the same Azimuth from the true meridian. So haue you the eleuation of the Pole, and situation of the meridian.

Now if you compare the Horizontall distance of the Azimuth of the Sunne, from the meridian at the tyme of the obseruation, with the variation by the Sunnes shadow found vpon the instrument, at the tyme of the same obseruation, and takyng the one out of the other, the remainer shalbe the true variation, whiche you are to accompte, as in the latter ende of the third Chapter is shewed. So haue you giuen the eleuation of the Pole, the meridian, and Variation of the Needle, the thynges proposed to be shewed.

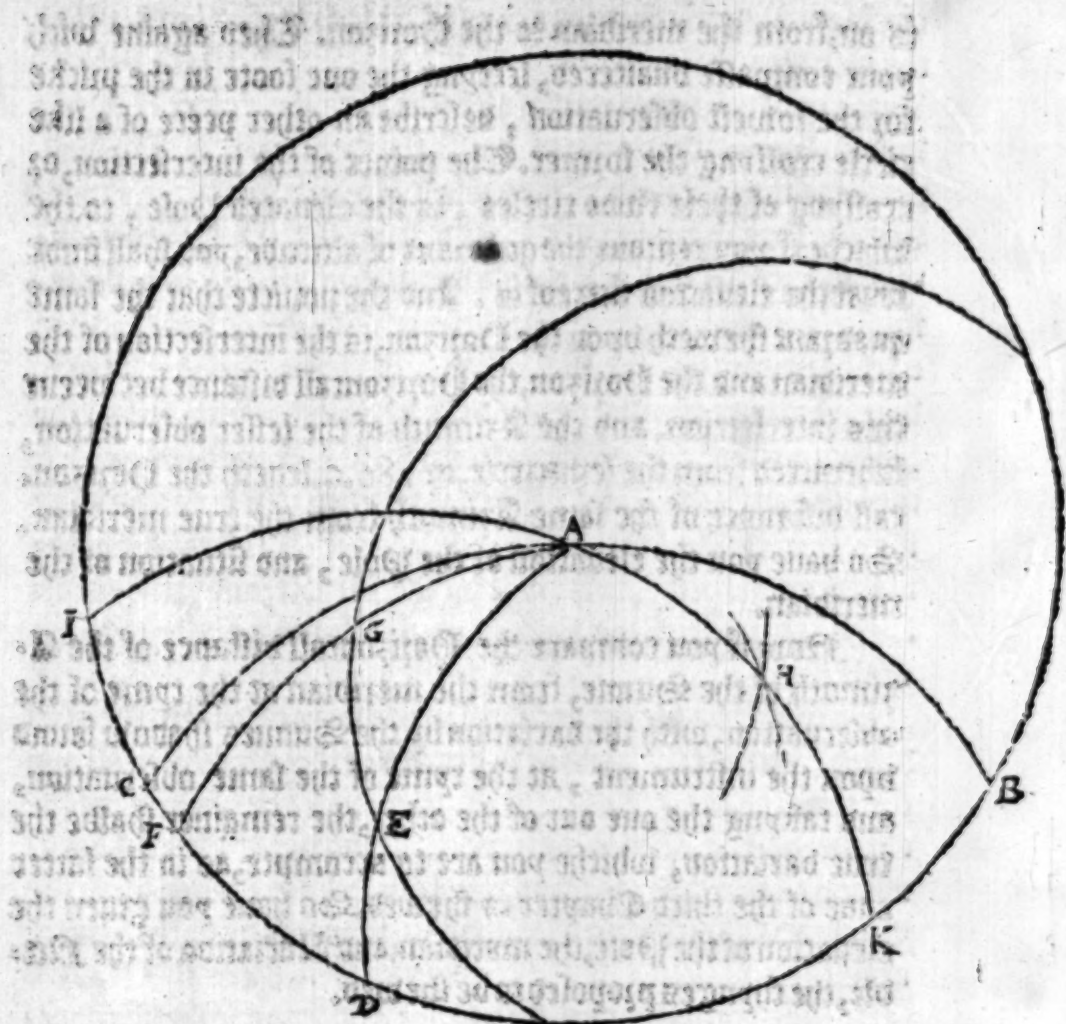
Example of twoo obseruations made

at Limehouse the 29. of Iulie 1581.
in the forenoone.

The first eleuation 21.d.0'. Variation 100.d.30'. from North to Weste. The seconde eleuation 50.d.0'. Variation 48.d.0'. from North to Weste. Difference of the Azimuths 52.d.30'. The declination 16.d.14'. Northerly.

LEt I D B. be the Horizō of the Globe. C A B. the meridian circle. F G A. the Azimuth of the greater eleuation shewed by the quadrant of altitude vpon the Horizon at F. 10.d. from the meridian circle of the Globe C. F G. the

of the Cumpas,



the greater eleuation marked vpon the Globe at G. FD.
the difference of the Azimuths vpon the Horizon, 52.d.30.
E, the prick of the lesser eleuation marked vpon the Globe in
the Azimuth A E D.

Then opening your Compasses to 73.d.46'. of the Equinoctiall (which is the complement of the declination) and setting one ende vpon G. the point of the greater eleuation, describe with the other ende, an ark or peece of a circle at H.

This done, set one foot of the Compas unaltered in E. the lesser elevation, and with the other end describe a piece of a

E.g. circle

Of the Variation

circle crossing the former ark at H. this intersection shall bee the elevated Pole.

Then set the quadrant of altitude vnto the point H. and it will shewe the meridian to crosse the Horizon at K. So shall you haue the eleuation of the Pole KH. $51^{\circ} \frac{1}{2}$. or there about. And the true meridian K A I. And from K. to D. the Horizontal distance $90^{\circ} \frac{1}{2}$. which subtracted from KI. 180° . the semicircle of the Horizon, resteth the ark D I. $89^{\circ} \frac{1}{2}$. the distance of the Azimuth of the first obseruation from the meridian I. which distance compared with the variation found vpon the Instrument at the first eleuation $100^{\circ} \frac{1}{2}$. and deducted from the same, resteth $11^{\circ} \frac{1}{2}$. Therefore I say, the true meridian shewing the Pole Arktik is $11^{\circ} \frac{1}{2}$. to the Westwards of the magneticall meridian shewed by the Needle, and consequently the variation of the Needle $11^{\circ} \frac{1}{2}$. from the North to the East.

In this example the declination is subtracted from the quadrant, because the Sunne is betweene the Equinoctiall and the elevated Pole, but if the Equinoctiall were betweene the elevated Pole, and the Sunne then should you adde the declination to the quadrant, and with that distance taken vpon the Equinoctiall with your Compasses, proceede as in the former example

These examples that I haue shewed, and suche like experiments to be done vpon the Globe, are easie to be conceiued, and the reasons very manifest: but the truth of the matter consisteth in the exactnes of the Instruments, and the orderly application and handling of them.

I might here haue annexed the maner, how vpon two obseruations of the Sunnes eleuation in fornoone or afternoone and difference of the Azimuths, to calculate the premisses more exactly by the table of Sines and doctrine of sphericall triangles: but that it is a very tedious way, and my meanning is rather to giue the Reader a proof of the pleasant vse of these calculations (whiche I thinke I haue sufficiently done in the former Chapters) then to cloy hym at the first with the hard
and

of the Cumpas.

and painfull practise of many examples. Notwithstanding, for the satisfaction of some, I will briefly set downe the grounde and summe of the work, which is this.

The complements of your two eleuations, are two sides of a sphericall triangle not rectangle. The angle by these two known sides containd at the Zenith, is giuen by the difference of the Azimuths or variations vppon the Instrument. Wherefore by the 28. of the 4. of Regiomontanus the third side (whiche is the arke comprehended betweene the two eleuations) and the other angles may be giuen.

Then haue you an other like triangle, whose three sides are these: the first, one of the foresaid complements of eleuation: the seconde, the arke of the circle of declination, betweene the Sunne at the instant of the same eleuation, and the eleuated Pole. The third side is an arke of the meridian betweene the Zenith and the Pole: whiche is the complement of the eleuation of the Pole, or latitude of the place. The two first sides are alwaies giuen. For finding the third side, it is necessarie to knowe the angle that the two giuen sides containe, whiche is the difference of two angles, whereof one is an angle of the first triangle giuen, the other an angle contained betweene the arke of the circle of declination, and the third side of the first triangle, whiche angle is diuersly founde, and being founde and subtracted from the other angle, or that from it, the difference is the angle of this other triangle: And so haue you in the Sphericall triangle two sides, and the angle by the same two sides contained, giuen. And by the same 28. of the fowerth of Regiomontanus the thirde side is found, the complement whereof is the eleuation of the Pole.

And the eleuation of the Pole, and declination of the Sun being giuen, the fowerth Chapter sheweth by one obseruation, to finde the Variation of the Needle.

Eiij.

Of

Of the Variation

Of the Pole of the Magnes.

The eight Chapter.

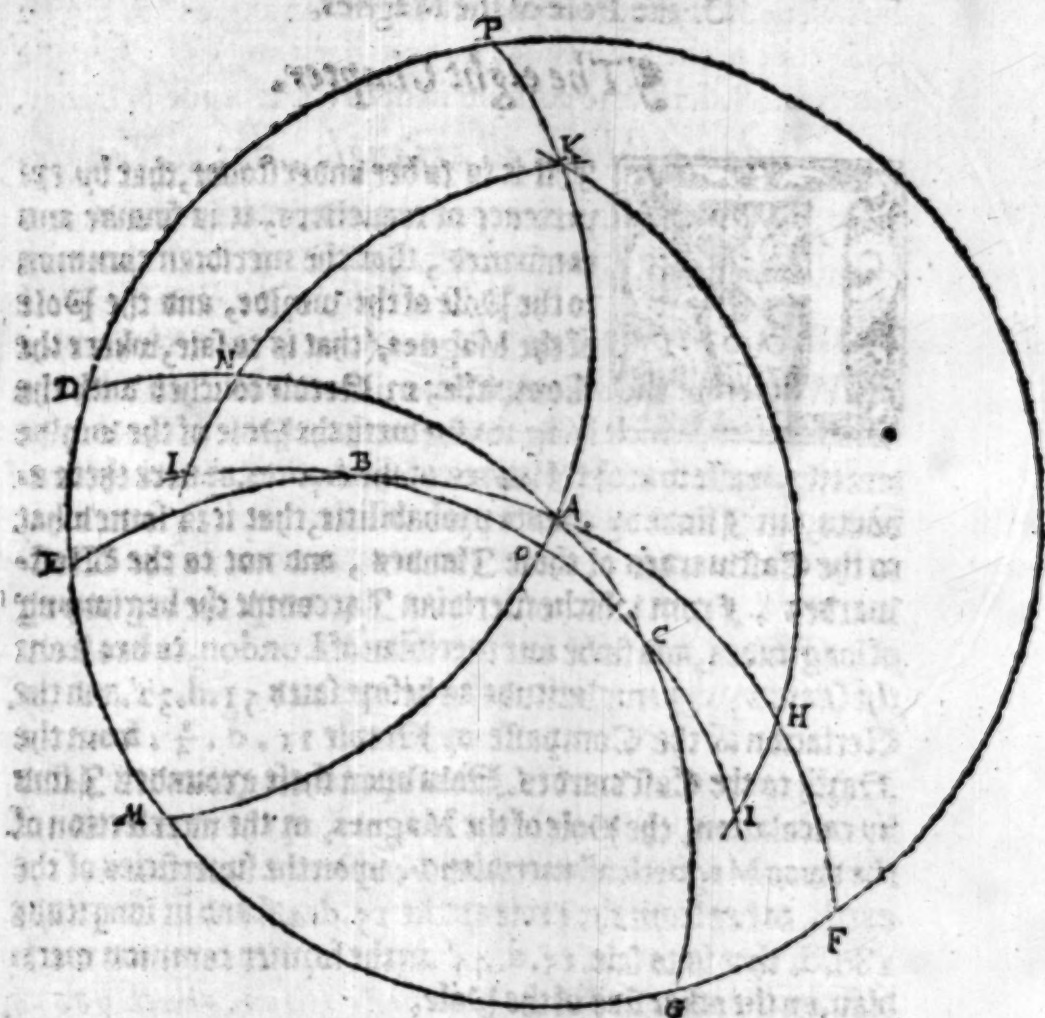


First it is to bee understoode, that by experience of travellers, it is founde and confirmed, that the meridian common to the Pole of the worlde, and the Pole of the Magnes, (that is to saie, where the Compasse, or Needle touched with the Magnes, sheweth the Pole of the worlde directly,) passeth at the Ilandes of the Açores, or nere there aboute, but I finde by greates probabilitie, that it is somewhat to the Eastwardes of those Ilandes, and not to the Westwardes. From whiche meridian I accompt the beginning of longitudes, and finde our meridian of London, to bee from the same $23^{\circ}.45'$. our latitude as befoze saied $51^{\circ}.32'$. and the Variation of the Compasse or Needle $11^{\circ}.15'$. from the North to the Eastwardes. Now upon these groundes I find by calculation, the Pole of the Magnes, or the intersection of the twoo Magneticall meridians, upon the superficies of the earth, to bee from the Pole artike $25^{\circ}.44'$. and in longitude 180° . that is to saie, $25^{\circ}.44'$. in the former common meridian, on the other side of the Pole.

It maie bee happely that some of you will bee desirous to knowe the maner how this Magneticall Pole is founde out, that you maie apply the same to like purpose hereafter. Therefore I thought good to sette downe an example of the former calculation.

Let A. bee the Pole Artik. PEF. the Equinoctiall.
DAG. the common meridian of the Pole Artik, and Pole of the Magnes. EAF. the meridian of London.
LOI. the magneticall meridian for London. B. for the place of London. HI. the quantitie of the angle of Variation at the ende of the quadrants BH. and BI. C. the intersection

of the Cumpas.



section of the two magneticall meridjans. CL, and C N, two quadrants of the said magneticall circles, including the ark L N. the quantitie of the angle at C. P A M. the Semi-circle of a meridian crossing the magneticall meridian of London in the point O. at right angles.

Make out the quadrants I H K. and L N K. so shall they crosse them selues with the quadrant O A K. at the point K.

Now haue you A B C. a sphericall triangle, two angles whereof and the common contaynyng side of them, are giuen. A B C. $11, d. \frac{1}{4}$, the angle of Variation at London.

BAC.

Of the Variation

BAC. 156.d. 30'. the complement of the angle DAE. (the difference of the longitudes) to two right angles. And the side AB. 38.d. 28'. the complement of the latitude of London.

And in a sphericall triangle, not rectangle, whose two angles are giuen, and their common contaynyng side, the other angle and sides shalbe knownen, by the 31. of the 4. of Regiomontanus.

Wherefore the arke AC. the distance of the two Poles shalbe giuen, which is the thyng required.

For as the sine of BH. is to the sine of HI. so is the sine of BA. to the sine of AO. and three of them beyng giuen the 4. is found.

90.0'.	11.15'.	38.28'.	658'.
BH.	HI.	BA.	AO.

If. 100000. giue. 19509. — then. 62205. giue. 12135.

Now as AK. is to AH. (the sines I meane) so is KO. to OI. but the three first are knownen AK. and AH. by their complements, and KO. the quadrant. Therefore the 4. is giuen.

83.2'.	51.32'.	90.0'.	52.4'.
KA.	AH.	KO.	OI.

If. 99261. giue. 78297. — then. 100000. giue. 78879.

And as BA. is to BO. (the complement of the arke OI. last founde:) so is AE. to EM. the quantitie of the angle BAO.

38.28'.	37.58'.	90.0'.	81.12'.
AB.	BO.	AE.	EM.

If. 62205. giue. 61474. — then. 100000. giue. 98824.

So hauing EM. 81.d. 12' the quantitie of the angle BAO. I subtraet the same from EG. 156.d. 30'. the quantitie of the whole angle BAC. rest MG. 75.d. 18'. the quantitie of the angle CAO. so the which is equall the opposit angle PAD.

And

of the Cumpas.

And as AP is to PD , so is AK , to KN .

90.0'.	75.18'.	83.2'.	73.48'.
AP .	PD .	AK .	KN .

If, 100000. gine. 96726. — then, 99261. gine. 96011. 1

The complement of whiche ark KN , is NL , 16. d. 14. the quantitie of the angle ACB . And as NL , is to NC , so is AO , to AC . Wherefore I say.

16.14'.	90.0'.	6.58'.	25.44'.
NL .	NC .	AO .	AC .

If, 27954. gine. 100000. — then, 12135. gine. 43410.

Which is the distance of the Pole of the Magnes from the Pole Artike: the thyng that was sought.

¶ Of the point Respectiue.

The ninth Chapter.



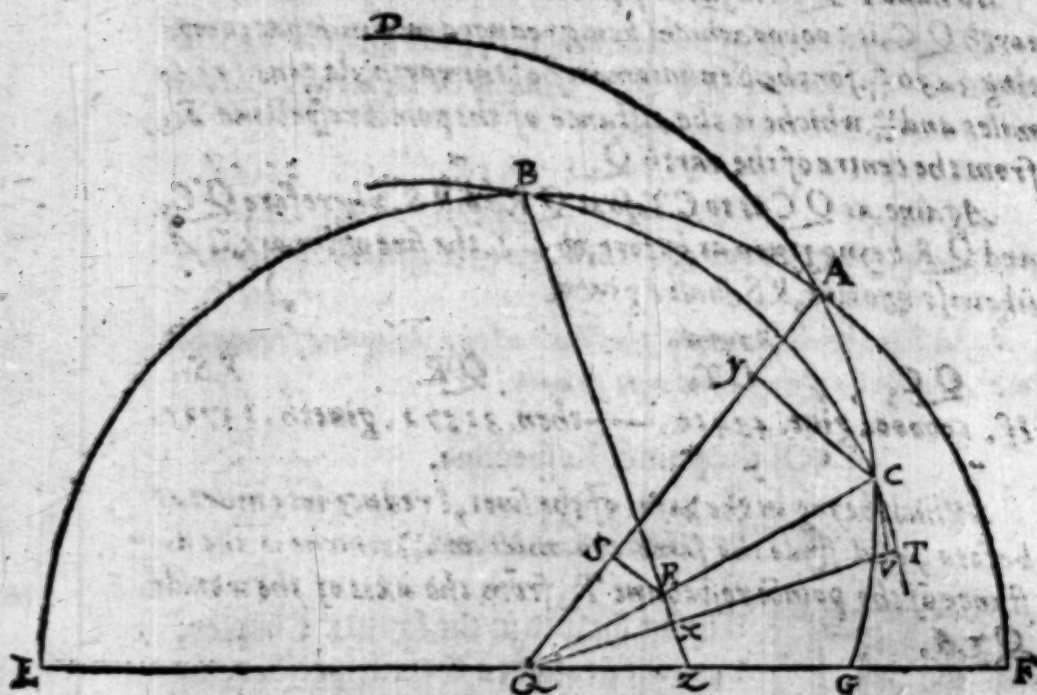
Anyng shewed in the former Chapter, vpon the groundes therein specified, the place of the Pole of the Magnes, vpon the superficies of the earth: there resteth now to bee declared, of the pointe Respectiue, where it should be, by the newe proprietie founde of the declining of the Needle, at this place for London 71. d. 50'.

First it is to bee considered, that as the Magneticall meridians doe crosse them selues at their Pole, before specified: so doe their plaines likewise crosse in a right line, passing by the saied Pole, and the centre of the earth. Then producing a straight line, in the Magneticall plaine of London, declining from the plaine of the Horizon 71. d. 50'. where the same both crosse with the former common section of the twoo plaines, there by reason should the point Respectiue bee. Whiche intersection I finde to bee from the centre of the earth 1085.

F. J. miles

Of the Variation

miles (after the rate of 60. to a degree in the Equator, and $3436\frac{4}{11}$. for the Semidiameter of the earth) and the distance of the same from the axis of the world 471. miles.



L Et the circles be as in the last demonstration. And **Q.** the centre of the earthe. Then **Q A.** the axis of the worlde. **Q C.** the common section of the magneticall plaines. **B Z.** the line of the Needles declination crossing the saied common section at **R.** whiche is the point respectiue. **Q T.** a straight line crossing **B Z.** at right angles in **X.** **Q R.** the distance of the point respectiue from the centre of the earth. **R S.** the distance thereof from the axis. Now as **Q V.** is to **Q C.** so is **Q X.** to **Q R.** But the three first are knowne. **Q V.** the seconde right sine of the ark **C T.** 9. d. 4'. (the difference of the ark **B T.** 71. d. 50'. And **B C.** 62. d. 46'.) Then **Q C.** the Semidiameter or whole sine, and **Q X.** the second right sine of the ark **B T.** Wherefore **Q R.** shalbe giuen, by the 4. of the sixt. of *Euclide.*

80.d.

of the Cumpas.

30.56. 90.0. 12.10.
 $QV.$ $QC.$ $QX.$ $QR.$
 If. 98750. gine. 100000. — then. 31178. gine. 31572.

So haue I $QR.$ in suche parts as the Semidiameter of the earth $QC.$ is 100000. which (being reduced into miles according 3436 $\frac{1}{11}$. for the Semidiameter of the earth) do gine 1084. miles and $\frac{10}{11}$. whiche is the distance of the point respectiue $R.$ from the centre of the earth $Q.$

Againe, as $QC.$ is to $CT.$ so is $QR.$ to $RS.$ wherefore $QC.$ and $QR.$ being giuen as before, & $CT.$ the sine of the arc $CA.$ likewise knowne, $RS.$ shalbe giuen.

25.44.
 $QC.$ $CT.$ $QR.$ $RS.$
 If. 100000. gine. 43410. — then. 31572. gine. 13705.

Which being in the parts of the sines, I reduce into miles as before, and finde the same 470. miles and $\frac{10}{11}$. whiche is the distance of the point respectiue $R.$ from the axis of the worlde $CA.$

¶ Of the Inconueniences and defects in sayling, and in description of Countries, caused by the Variation of the Cumpas.

The tenth Chapter.

In all sea chartes generally, whiche are made without consideration of the variation, are committed great errors and confusion. For, either the partes in them contained, are framed to agree in their latitudes by the scale thereof, and so wrested from the true courses that one place beareth from another by the Cumpas, or els in setting the parts to agree in their true courses, they haue placed them in false latitudes, or abridged, or ouer stretched the true distances betwene them.

F. 11.

In

Of the Variation

In the Marine plattes made for Newfoundland, the course sette downe from Silly to Cape Rasó is due Weste, whiche is founde to bee so by our common sayling Compass, whose wiers are sette at $\frac{1}{2}$, a point from North to East, notwithstanding Silly being in latitude 50.d. little more, Cape Rasó in Newfoundland is founde to bee but in 46.d. $\frac{1}{2}$, which is 3.d. $\frac{1}{2}$. lesse then the latitude of Silly.

To make a shew of reformation of this error, (caused by the Variation and setting of the wiers in the Compass) by to give a light of that difference in latitude, they have placed in the plat against that coaste, a newe scale of latitude, some vpon the line of South and North, and some other haue placed the same vpon the line of North Northeast, & South South Weste, (because that point of the Compass betwix the Pole nere is in that place) and haue furnished the degrees thereof, agreeably to the latitude of Cape Rasó: and by that meanes haue had a double scale of latitude, one for the Easter coastes, the other for that Weste. But how farre the same hath been from reforming the error, by giuing any helpe to Navigation, you maie easily iudge.

Others to auoide that error of the difference in latitude in that voyage and course, haue used Compasses whose wiers haue been sette directly vnder the North point, and thereby sayling Weste from Silly, haue fallen to the Northwardes of Cape Rasó about 50. leagues, and in latitude nere 49.d.

Some other haue used in the same voyage to place a blank Flye vpon their sayling Compass, whiche they haue remooued from tyme to tyme, as they haue iudged the variation hath altered, by whiche waie, albeeit they maie seeme to keepe them selues neerer the parallell, yet the same in Navigation worketh the greatest confusion of all other, and therefore is to bee utterly abolished.

In our voyages from hence Eastwardes to S. Nicolas in Russia, and to the Narue in Liuania &c. the Marine plattes of the coastes are described by our common sayling Compass, with consideration of the variations at diuers places, where-

by

of the Cumpas.

by the true meridians reformedly set doune, declining from þ parallel meridians of the plat, doe necessarily widen Northwardes, and straighten to the Southwardes, contrary to the true forme and nature of meridians. And yet notwithstanding, that is the best meanes hether to knowen, to reforme the plat, the errors that els would growe, by the strange variations that waile.

And albeit these plattes serue verie well for those Navigations, yet by meanes of the variations considered, the forme of those coastes is so distorted from the right shape it should beare, being truly described vpon the Globe or otherwise in plaine, according to the true latitude and longitude: That whereas the Narue (being in latitude $59^{\circ}.4'$, and in longitude from the meridian of London $26^{\circ}.10'$.) should be from S. Nicolas $9^{\circ}.40'$ in longitude to the Westwardes (S. Nicolas being in latitude $64^{\circ}.35'$ and in longitude from London $35^{\circ}.50'$.) In the sayling plat it is brought to be in the meridian of Colmogorod, (whiche is in latitude $64^{\circ}.20'$ and in longitude from London $37^{\circ}.45'$.) whiche is $1^{\circ}.55'$ to the Eastwardes of the meridian of S. Nicolas.

In the Mediterranean Sea, and in the coastes thereof, where, in great reason should be the perfectest descriptions of the world, for that in those parts haue been the seates & abodes of the most famous and learned men in all ages, we see notwithstanding in the Marine plattes of those partes, grosse errors committed, through want of knowledge of the variation and the vse thereof, in whiche they haue not accounted of $3.4.05$ degrees error in the latitude of places.

But those defectes of the latitudes, haue been verie well reformed, by the famous and learned Gerardus Mercator (whom I honour and esteeme as the cheef Cosmographer of the world) in his vniuersal Map, which though he haue made with sayling lines, and dedicated to the vse of Seamen, yet for want of consideration of the Variation, and partly by augmenting his degrees of latitude towardes the poles, the same is more fitte for such to beholde, as studie in Cosmographie, by

Of the Variation

readyng aucthoures vpon the lande, then to bee vsed in Navigation at the sea.

There is also in the same Uniuersall Mappe, and likewise in all other moderne Mappes of the North partes of Europe, a greate fault, by placing two Wardhouses distant one from the other about 20. d. in longitude, whereas in deede they are but one thyng, and no suche distance betweene them. This error hath growen by taking Wardhouse, and the Sea coastes, from thence to S. Nicolas, Vaigars and the Ob &c. out of the Mappe of Anthony Ienkinsons trauaile to Boghar and Persia. In the whiche I placed that border of the Sea coaste, and for some causes went no further in that description then Wardhouse, whiche is in latitude 70. d. 4. and in longitude from London 29. d. Wherefore to accomplishe the whole border of that coaste, he was forced to seeke some other description to ioine with it, & tooke as appeareth the Mappe of Olaus Magnus of the North countreies, wherein he found likewise Wardhouse, but falsly placed, in latitude about 19. d. too much, and in longitude as much too little, the which, although he might take to bee the same specified in Maister Ienkinsons Mappe, yet he was constrained to separate the the saied distance of 20. d. in longitude (or to leaue there so much superfluous roome) or therwise he should haue thrust the South partes of those countreies together, and confounded the whole description.

And albeit he had had the entire sayling plat, that wee vse for those partes, yet if he had not knowen the secret effect of the Variation in the making thereof, he might haue fallen into the like absurditie or worse. But of those coastes and of the inwarde partes of the countreies Russia, Muscouia &c. I haue made a perfect plat and description, by myne owne experience in sundrie boiages and trauailes, bothe by Sea and Lande to and fro in those partes, whiche I gaue to her Maiestie, in Anno 1578.

Besides these and like imperfections proceeding of the Variation, there is yet an other inconuenience, whiche oftentimes encreaseth the former errors, and that is, the diuers placing

of the Cumpas.

placynge of the wiers fixed to the Flie of the Cumpasse.

This varietie of setting the wiers, hath caused greates confusion in Navigation, and in other accomptes of Sea causes, for when it is said, that from suche a headlande, to suche a place is suche a course, or at suche a place the Poone vppon suche a pointe of the Cumpasse maketh the full Sea, it is requisite to bee demaunded, by what Cumpasse the obseruation was made, whereas if the wiers had not been altered from the North pointe of the Flie, (whiche I wishe had neuer been any where) these doubtcs had been auoided.

It behoueth therefore all men that will make Hydrographicall discriptions for the vse of saylyng, to haue speciall regard of the Cumpas by which their obseruations are made, and if they collect notes made by sundry Cumpasses of diuers setts, they ought to reduce all the varieties vnto some one certaine, and to giue notice of the same, in their platt: And not to make a confused mingle mangle by ioyning together all varieties of obseruations, notes and reportes, as the Portingales and Spaniards haue done, in compoundyng these North parts of the worlde, with their owne discoueries, without consideration of the diuers sortcs of the seuerall cumpasses by which they were made.

Also it importeth all Maisters, Pilots and others by what name so euer that shall giue directions in Navigation, to looke circumspectly to the setting of the wiers of the Cumpas by whiche they shall sayle, that the same Cumpas be correspondent, to the lynes of the Sea Card that they shall vse: that is to say, that it be of the same set for the Variation, that the Cumpas was of, by which the Carde was made.

And sayng wee haue in this our Countrey acquainted our selues commonly in our obseruations and Navigations, with the Cumpas, whose wiers are set at $\frac{1}{2}$, a point from North to East, I meane in the discriptions that I shall make, to apply the same agreeable to the said Cumpas, and would vse the like without alteration (and also the straight lines in Sea Cardes) if I should sayle rounde about the world to make the
description

Of the Variation

description thereof, but alwaies with regarde of the severall variations of every place where the same should be observed.

Of the Instruments and rules of Navigation.

The eleventh Chapter.



Amongst the rules and Instruments for Navigation, all suche are vaine and to small purpose, wherein the true meridian is presupposed to be given by the magneticall Needle, without due consideration of the variation for that they are all grounded vpon false suppositions. Hereby it cometh to passe that one Michiel Coignet of Antwerp in his New instruction (as he termeth it) of the most excellent and necessary points of Navigation, wherein he sheweth the making and vse of a Nautical Hemisphere, which he preferreth before all other Sea Instruments, is very childishly abused. For where as he pretendeth by it, to give the elevation of the Pole and the houre and instant of the tyme of the day, by any one observation in any place, besides that it is of all other that hitherto have been used at Sea, the most tedious and unfit for that purpose, it is also by reason of the variation not considered, mere false and erroneous. For, the true meridian which is the ground of his purpose, is as farre to seeke as the thing he promiseth to give by the same. The like may be said of al other Instruments made vpon the same ground whether they serue for the Sea or Land.

The same Author in the 4. Chapter of his booke, entreting at sayling vpon the points of the Cumpas, saith, that in sayling South or North, he shall passe by the Poles of the world, and keepe vnder one meridian, till he come to the place from whence he first departed. And vpon the points of East and West out of the Equinoctiall, he shall saile vnder a parallell, till he returne to the place from whence he went. But in sayling

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lyng vppon the poinct of Northeast, he shall describe a spirall line inclynng by little and little towards the Pole, as in his demonstration thereof in the same Chapter appeareth. But for want of due consideration of the variation, his rules, reasons and demonstrations, and suche others hitherto giuen for like purposes, are frivulous and false.

For if he direct his saylyng by the Cumpas (as of necessity he must, being the onely Instrument for that purpose) it is manifest, that whether he sayle North or South, East or West, or by what other poinct so euer, the Cumpas not respectyng alwaies the Pole of the world, as he supposeth, but some other poinct or poincts distant from the same, shall leade hym accordyngly, whereby he shall neither keepe vnder one meridian, nor vnder one parallell of latitude, neither make such a spirall line to the Pole of the world, as he demonstrateth. His fault in setting downe those rules is so muche the greater, in that he acknowledgeth in the Chapter next before the variation at Antwerp, to bee about 9.d. from North to East accordyng to Mercators position, of the Magneticall Pole, which he also confirmeth by his owne experience.

But it seemeth he hath followed, that excellent Mathematician Petrus Nonius, especially concernyng the saylyng vppon the poincts of East and West. For he, in his first booke of the rules and Instruments of Nauigation, enforceth hymself to proue and demonstrate, that in saylyng East or West, out of the Equinoctiall, the course is performed by peeces of great circles, and yet describeth a parallell. But how that may stande wiche the principles of Geometry, I referre the iudgement to the expert Mathematicians, for it is like as a circle should be made of straight lines, which is impossible.

It appeareth in the discourse that he hath made of those matters, that he had not a right iudgement of the nature of the Cumpas in saylyng (admitting the same to shew the Pole without Variation) for if he had, he would neuer haue entred into suche a Labyrinth as he did. But he thought it a great absurditie that the Cumpas in euery Horizon should shewe the

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meridian and Poles of the world by the pointes of South and North, and by the pointes of East and West to the we in the Horizon the verticall and Equinoctiall East and West (being a great circle) and yet in saylyng East or West, except in the Equinoctiall, it should performe but a parallell.

But it is to be understood, that albeit the pointes, or lynes of the Cumpas doe alwaies in euery Horizon represente great circles in the Heauens, the pointes of South and North the meridian, and the pointes of East and West the verticall circle of East and West, eche crosseing other at right angles, and likewise of the other pointes. (The reason whereof is, because the Cumpas lieth euery where leuell with the Horizon, so as a perpendicular line descendyng from the centre thereof at right angles with the plaine of the same, will alwaies fall vpon the centre of the earth, and consequently be the Semidiameter of a great circle.) So that where so euer the Cumpas be caried, these circles are supposed to be caried about with it, and the view of euery thyng in the Horizon represented by the pointes thereof, is likewise in great circles: Yet in saylyng by the Cumpas, the pointes of South and North onely, describe great circles generally, which are the meridians, & the pointes of East and West, describe a great circle in the Equinoctiall onely: in all other places out of the Equinoctiall, they describe but parallells. And the saylyng vpon any other point of the Cumpas, from any place, describeth a spirall line, according to the angle it maketh with the meridian. And hereby in saylyng vpon the pointes of East or West, out of the Equinoctiall, (the North point alwaies respectyng the Pole) the course performeth a parallell, accordyng to the distance of the centre of the Cumpas from the Pole. The maner thereof you may perceiue by fastnyng a small threed or Virginall wier at the Pole of a Globe, or centre of a circle, which shall represent a moueable meridian to bee caried about the Globe or circle, and fixe vpon the same, a small fflye of a Cumpas, so as the line of South and North be answerable to the threed or wier, and the North point thereby alwaies respect the North Pole; then

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in turnyng the threed about the Globe or circle, vpon the Pole or center, if the center of the Flye bee out of the Equinoctiall (between it and the Pole) albeit the points of East and West crossyng the same line and moueable meridian at right angles, doe shewe the verticall East and West vpon the Globe, which is a great circle, yet in cariyng the same Flye vpon the threed or moueable meridian, about the Pole or center, you shall by the center of the same Flye, describe but a parallell, accordyng to the distance thereof from the Pole of the Globe, or center of the circle, not vnlke the circular motiō of a Horse drawyng in a mill, who though he looke forth straight in a right line, yet beyng fastned to the beame of the mill, is forced to make his course in a circle, whose Semidiameter is the length of the beame contayned betweene the Horse, and the centre of the mill, or millpost.

And as in the Equinoctiall, the line of South and North in the Cumpas (by supposition representing the meridian) is parallell to the Axis of the earth (which is the common section of all the meridian plaines) and the line of East and West crossyng the same Axis at right angles, representeth the verticall East and West, which is the Equinoctiall, imaginypng to descende from the centre of the Cumpas a line, to fall perpendicularly, and at right angles with the Axis of the worlde (whiche shall bee at the centre of the earth) and in saylyng East or West by the Cumpas, the imagined perpendicular line being caried about with the same (makypng alwaies right angles with the Axis) shal describe the plaine of the Equinoctiall equidistant from the Poles of the worlde, and at right angles with the Axis, and the poince of the same line at the centre of the Cumpas, the circumference of the Equinoctiall, vppon the superficies of the Sea: So beyng from the Equinoctiall on either side, imaginypng the line of South, & North in your Cumpas to represent alwaies the Axis of the worlde, and to lye parallell with it, the line of East and West must crosse the same Axis alwaies, at right angles: and supposing a line to fall from the centre of your Cumpas to the Axis of

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the world, making right angles with the same Axis. In say-
ing East or West, that imagined line beeing carried about
with the Cumpas (alwaies at right angles with the Axis)
shall describe the plaine of a parallell, equidistant to the plaine
of the Equinoctiall, and the point thereof at the centre of the
Cumpas, the circumference of the parallell vppon the super-
ficies of the Sea: which parallell should be represented by the
points of East and West of the Cumpas, if the line of South
and North of the same were parallell to the Axis of the earth,
as was supposed: but it is not. And therefore as they decline one
from the other, so doeth the verticall circle of East and West
shewed by the Cumpas, decline from the parallel circle every
where.

The angle of whiche declination, is alwaies equall to the
latitude of the place, or distance of the parallell from the Equi-
noctiall.

But as I haue already sufficiently declared, the Cumpas
sheweth not alwaies the Pole of the worlde, but varreth from
the same diuersly, and in saying describeth circles accordyng-
ly. Whiche thynge if Petrus Nonius and the rest that haue
written of Nauigation, had ioyntly considered in the tracta-
tion of their rules and Instruments, then might they haue
been more auailable to the use of Nauigation, but they per-
ceiuing the difficultie of the thynge, and that if they had dealt
therewith, it would haue bitterly ouerwhelmed their former
plausible conceits, with Pedro de Medina (who as it appea-
reth hauing some small suspicion of the matter, reasoneth ve-
ry clerkly, that it is not necessary that such an absurdity as the
Variation, should be admitted in such an excellent art as Na-
uigation is) they haue all thought best to passe it ouer with si-
lence. But I hope suche as intende hereafter to write of Na-
uigation, will either frame their rules, precepts, and Instru-
ments, with regarde of the Variation, as herew I haue shew-
ed, or els ease them selues of that trauaile, for as good none
as unprofitable.

of the Compas.

Of the application of the Variation to the vse of Navigation.

The twelfth Chapter.



Upon the Hypothesis of the Pole of the Magnes on the superficies of the earth, and the poinct Respectiue in the body thereof, according to the former calculations, might be inferred many pleasant conclusions, both for the longitude and latitude of places.

But touching the poinct Respectiue by the declining of the Needle, seeing this is the first and onely experiment that hath been made of it, I can not inferre any further matter thereof, then that whiche I haue already set downe, vntill by obseruations in other places, we finde how it will holde.

And as for the Variation, if it were generally regular and certaine, as in some part it seemeth to be: (that is to say, from hence Westwardes to Meta Incognita, New foundland, Florida, and that part of the coast of America) then might there be giuen by it generall rules most certaine and commodious for the vse of Navigation.

And by the same Hypothesis of the Pole of the Magnes at 25.44 . from the Pole of the world, the greatest variation of the Needle in the Equinoctiall, should be (at $90.d.$ of Longitude) 25.44 . from North to East. And consequently the greatest variation in the parallel of $70.d.$ should bee (at the longitude of $128.d.51'$) from North to East $81.d.14'$. And in the meridian of $180.d.$ of longitude between the two Poles, (the Pole Arctic I meane, and the supposed Pole of the Magnes,) there should the North poinct of the Needle or Compas respecting his own Pole, shew the South, and the South poinct, the North Pole of the world.

But in my trauelles to the Northeest parts, I haue found this position of the magneticall Pole cleene reuerfed: for where

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as the angle of Variation from hence Eastwardes in the parallel of 70.d. should encrease and growe wider, till it came to 81.d. 14'. from North to East as before. At the Island Vaigats being in longitude from London 58.d. and in the same parallel of 70.d. where, by the Hypothesis, the variation should be 49.d. 22'. from North to East, I finde the Needle to vary 7.d. from North to West. And the like effect I haue found by diuers obseruations in sundry other places of the East partes. Whiche obseruations with many more that I haue caused to bee made, and dayly procure to be done in diuers other Countries, I reserve, with intent (if it bee possible) to finde some Hypothesis for the saluyng of this apparant confused irregularitie.

At Ratisbona or Regensburg in Bauaria, being in latitude 48.d. 52'. and in longitude 36.d. 20'. where, by the former position of the magneticall Pole at 25.d. 44'. the Variation should be 16.d. 44'. from North to East. Gerardus Mercator found the same to be onely 11. $\frac{1}{4}$. as I gather by his placing of the magneticall Pole at 16.d. 22'. from the Pole Artik upon his obseruation made at that place: whiche confirmeth the retrograde qualitie in the Variation from hence Eastwardes, as aforesaid.

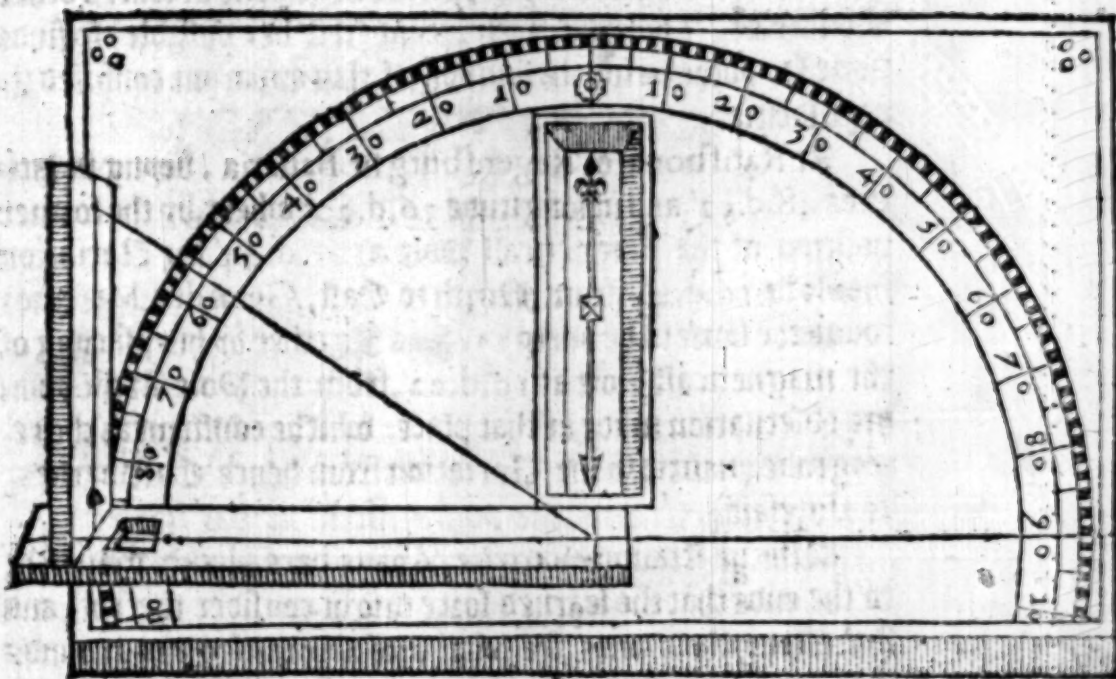
Whiche straunge varietie, I haue here plainly proposed, to the ende that the learned sorte might consider thereof, and sharpening their wits, see what probable causes and grounds they can assigne for the same. For, considering it remaineth alwaies constant without alteration in euery seuerall place, there is hope it may be reduced into method and rule.

As for that Westwardes, because it carrieth proportion, and hath some apparant regularitie, I will apply the same to the generall commoditie of all suche as shall trauaile that wates: which if I should here particularly decipher, it would require a volume, whereby (contrary to my first intent) I should farre exceede the bounds of an addition, I will therefore abridge it to a Hydrographicall Plat, wherein all such errors and defects as haue been hitherto used, shalbe reformed, whiche

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which shall be easy for the meaneſt capacities to conceiue, and ſerue more effectually in uſe, then if I ſhould haue expreſſed the ſame by multitudes of rules in writing. Therefore for this matter I referre you to the ſame, the which you ſhall looke for very ſhortly.

A new Inſtrument for the Variation,



BEcauſe I haue found ſonie imperfections in the firſt Inſtrument for the Variation (which notwithstanding any dyng doeth farre excell the Cumpalles of Variation heretofore vſed for that purpoſe) I haue here ſet ſowne the forme of a newe Inſtrument, wherein all ſcruple of doubts and defects that might growe by the other is quite auoyded. Which being once exactly placed with the Needle vpon the line of South and North, will ſerue without remouing for a whole daies obſeruatiō, the Index onely being caried about with

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with the Sunne, to give the degrees of Azimuth vpon the Instrument by the shadowe of the line thereof, and is otherwise to be vsed accordyng to the prescript rules of the former Instrument.

These Instruments are made by Robert Norman, and may be had at his house in Ratclif.



Imprinted at London for Richard
Ballard, and are to be solde at his shop
at Saint Dagnus corner in Thames
streete. Anno. 1581.



